

Acoustically camouflage

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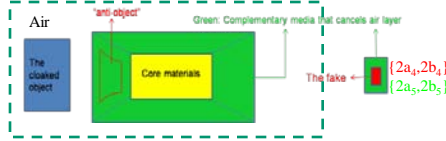
Motivation

- ✓ Conceal an object at one place and emerge at another place
- ✓ Many potential applications. For example, mislead enemy to make a chance to steal with submarines

Our train of thoughts

- Acoustically conceal the object A with an acoustical cloak
[For remote electromagnetic cloaks, see PRL 102, 093901 (2009)]
- Enhance the acoustically scattering capability of a smaller object B to get the same pressure distribution as A in the absence of the cloak
[For electromagnetic superscatterers, see Opt. Express 16, 18545 (2008)]

Rectangular version



Region size

Core material $\{2a_1, 2b_1\}$
Complementary media $\{2a_2, 2b_2\}$
Air $\{2a_3, 2b_3\}$

The coordinate transformation from the air layer to core region (yellow)

$$\begin{cases} x' = \frac{2a_1}{2a_3} x \\ y' = \frac{2b_1}{2b_3} y \end{cases}$$

The complementary media region is divided into 4 subdomains to accomplish coordinate transformation. For subdomain I

$$\begin{cases} x' = -\frac{a_3 - a_2}{a_3 - a_1} x - \frac{a_3 - a_1}{a_3 - a_2} a_2 \\ y' = -\frac{a_3 - a_2}{a_3 - a_1} y - \frac{a_3 - a_1}{a_3 - a_2} a_1 \end{cases}$$

$$\rho_{ij}' = \det(\Lambda)^{-1} (\varepsilon_{ijk} \Lambda_l^k \varepsilon_{lmn}^l) (\varepsilon_{jmn} \Lambda_i^m \varepsilon_{klm}^k) \rho_0$$

$$\lambda' = \det(\Lambda) (\Lambda_i^j)^{-2} \lambda$$

The mass density and bulk modulus obtained by using

$$\rho_{xx}' = \frac{(a_3 - a_2)^2 x'^4 + a_2^2 (a_3 - a_1)^2 y'^2}{(a_3 - a_1) x'^3 \Delta}$$

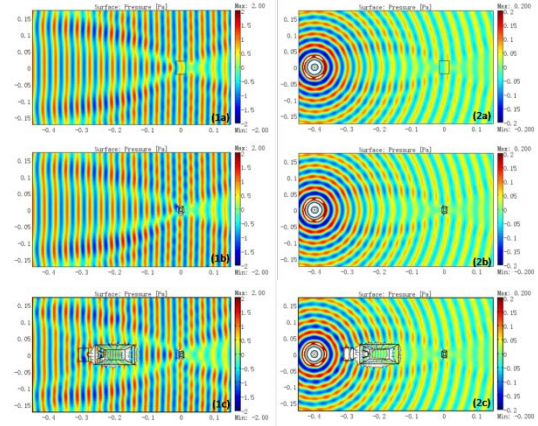
$$\rho_{yy}' = \rho_{xx}' = -\frac{a_2 (a_3 - a_1) y'}{(a_3 - a_2) x'^2}$$

$$\rho_{xy}' = \frac{\Delta}{(a_3 - a_2) x'}$$

$$\lambda' = \frac{(a_3 - a_1)^2 x'}{(a_3 - a_2) \Delta}$$

The coordinate transformation from the air layer to green layer subdomain I

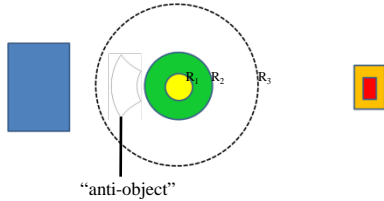
Simulation results of rectangular version



Snapshots of the pressure fields under an incident acoustic (1a)-(1c) plane wave, (2a)-(2b) cylindrical wave. (1a) and (2a) A rectangular object of size [0.03m, 0.04m]. (1b) and (2b) The scattered pressure field distribution of the rectangular object of size [0.0075m, 0.01m] is the same as the one of the object of size [0.03m, 0.04m]. (1c) and (2c) With a rectangular object on the left, the scattered pressure distribution is same to (1b) and (2b), respectively.

All objects have $\rho_0 = 5$ and $\lambda_0 = 16$.

Circular version

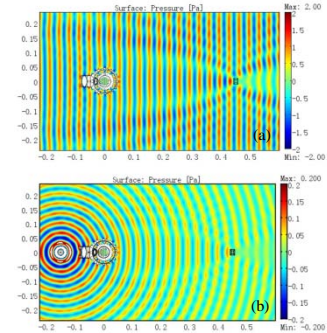


The coordinate transformation from the air layer to green layer

$$\begin{cases} r' = -\frac{R_2 - R_1}{R_3 - R_2} r + \frac{R_3 - R_1}{R_3 - R_2} R_2 \\ \theta' = \theta \end{cases}$$

Simulation results of circular version

Snapshots of the distribution of pressure fields under (a) an incident acoustic plane wave, (b) a cylindrical. Distributions of pressure fields of single object are similar to (1a),(1b),(2a) and (2b).



Discussion and conclusion

- With our design we can make a feint to the east but attack in the west (“声东击西”).
- All simulations obtained by using finite-element solver Comsol Multiphysics 3.5.

References

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- [2] J. B. Pendry, D. Schurig and D. R. Smith. Controlling electromagnetic fields. *Science*, 312: 1780-1782 (2006)
- [3] Y. Lai, H. Y. Chen, Z. Zhang, and C. T. Chan. *Phys. Rev. Lett.*, 102: 093901, (2009).
- [4] S. A. Cummer, D. Schurig. *New J. Phys.*, 9: 45, (2007).