# **Constructive coupling effect of topological states and topological** phase transitions in plumbene

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## Abstract

Combining tight-binding (TB) models with first-principles calculations, we investigate electronic and topological properties of plumbene. "Constructive" coupling effects of topological states are found in the low-buckled plumbene, causing the system being a normal insulator, opposite to topologically nontrivial states formed in other two-dimensional (2D) group IVA monolayers (from graphene to stanene). Local topologic states are found being located not only at the  $\Gamma$  point in the Brillouin zone, but also at the K/K' points, whose coupling determines the final topological behaviors of the whole system. Based on this mechanism, several schemes are raised to produce a globally topological state in the plumbene. When the plumbene is functionalized with ethynyl (PbC<sub>2</sub>H), a quantum spin Hall (QSH) state comes out. Very interestingly, when an exchange field is introduced to the pristine plumbene, the system exhibits a quantum anomalous Hall (QAH) effect despite the coupling effect of the topological states.







FIG. 2. (a) and (b) Orbital-projected band structures, and (c) edge states of plumbene.

#### **Coupling effect of topological states from tight-binding model**

**(c)** 

**Tight-binding model** 

$$H(\mathbf{k}) = \sum_{\langle ij \rangle, \alpha, \beta; \sigma, \sigma'} c^{\dagger}_{\alpha \sigma i} t_{\alpha \sigma i; \beta, \sigma' j} c_{\beta \sigma' j} + \lambda L \cdot S + M \sum_{i; \alpha; \sigma, \sigma'} c^{\dagger}_{\alpha \sigma i} s^{z}_{\sigma \sigma'} c_{\alpha \sigma' i}$$

**Topological properties** 







**(a)** 

(eV)



**(e)** 



300

200 (x) رواي (لا)

ي چ 100-

-150

-200

FIG. 3. (a) and (b) Band structures, (c) band structure when an exchange field is applied, (d) Berry curvatures in the 2D momentum space for the spin-up subspace, (e) and (f) Berry curvatures and bands for the spin-up and spin-down subspace, respectively, obtained from TB model.

### **Topological phase transitions**



FIG. 4. Schematic diagrams of the topological phase transitions.

FIG. 5. (a) and (b) Geometry structures, (c) and (d) orbital-projected band structures, (e) edge states, and (f) phonon band dispersions of PbC<sub>2</sub>H.

#### **References:**





#### 4. Y. Li, J. Zhang, B. Zhao, Y. Xue, and Z. Yang, Phys. Rev. B 99, 195402 (2019).