

# Dynamical magnetoelectric coupling in axion insulator thin films

Zhaochen Liu<sup>1</sup>, Jiang Xiao<sup>1, 2</sup> and Jing Wang<sup>1,2</sup>

<sup>1</sup>State Key Laboratory of Surface Physics and Department of Physics, Fudan University, Shanghai 200433, China <sup>2</sup>Institute for Nanoelectronic Devices and Quantum Computing, Fudan University, Shanghai 200433, China

### Introduction

### **Topological Insulator:**

Low Energy Action:

$$S = S_{Maxwell} + S_{Axion}$$

$$S_{Axion} = \frac{\theta}{2\pi} \frac{e^2}{2\pi\hbar c} \int d^3x dt \mathbf{E} \cdot \mathbf{B}$$

$$= \hbar\theta N$$

 $\theta = \pi$ : Topological Magnetoelectric Coupling Orbital Effect (Band Effect).

#### **Axion Insulator:**

**Axion Electrodynamics:** 

$$-\frac{1}{c^2}\frac{\partial \mathbf{E}}{\partial t} + \nabla \times \mathbf{B} = \frac{\alpha}{\pi c} \left( \dot{\theta} \mathbf{B} + \nabla \theta \times \mathbf{E} \right)$$
$$\nabla \cdot \mathbf{E} = -\frac{\alpha c}{\pi} \nabla \theta \cdot \mathbf{B}$$

TME Current:

$$\mathbf{j} = \frac{e^2}{2\pi h} \left[ \nabla \theta \times \mathbf{E} + \partial_t \theta \mathbf{B} \right]$$

For Axion insulator thin film, the  $\theta$  is not quantized and depends on thickness and surface gap.

$$1 - \frac{\theta(d)}{\pi} = \frac{\beta(\Delta_s)}{d} + o\left(\frac{1}{d^2}\right)$$
$$\eta \equiv (d/\pi)(\partial\theta/\partial\Delta_s)$$

Dynamics on surface gap would give  $\theta$  time dependence.

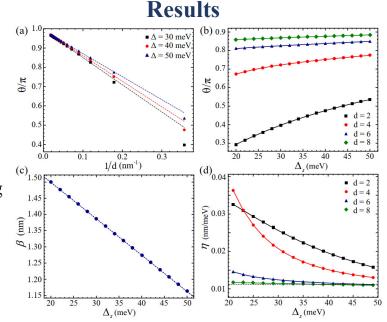
$$\partial_t \theta = \frac{\partial \theta}{\partial \Delta_s} \frac{\partial \Delta_s}{\partial t}$$

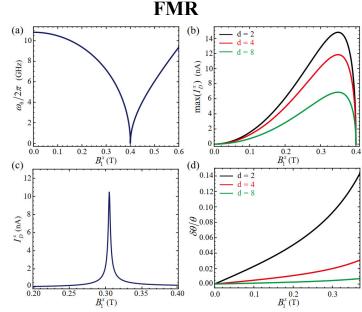
Surface magnetic resonance induced surface gap dynamics.

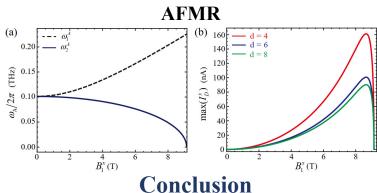
$$\mathcal{J}_D = \mathcal{J}_D^x \hat{\mathbf{x}} = \frac{e^2}{2h} \eta g_M \partial_t \delta M_z \left( B_1^x + B_2^x \cos(\omega t) \right) \hat{\mathbf{x}}$$

## Reference

- [1] X.-L. Qi and S.-C. Zhang, Rev. Mod. Phys. 83, 1057(2011)
- [2] X.-L. Oi, T. L. Hughes, and S.-C. Zhang, Phys. Rev. B78, 195424 (2008)
- [3] Liu Z, Xiao J, Wang J. Dynamical magnetoelectric coupling in axion insulator thin films. arXiv:2007.09869, 2020.







The surface magnetic resonance can induce dynamical magnetoelectric current in Axion insulator thin film.