

# Temperature-Dependent Transformation Multiphysics and Ambient-Adaptive Multiphysical Metamaterials

Min Lei<sup>1</sup>, Jun Wang<sup>1</sup>, Gao-le Dai<sup>2</sup>, Peng Tan<sup>1</sup> and Ji-ping Huang<sup>1</sup>

<sup>1</sup>Department of Physics, Fudan University, Shanghai 200438, China

<sup>2</sup>School of Sciences, Nantong University, Nantong 226019, China

**Introduction.** Recent advances in metamaterials and metadevices in diffusion systems [1,2] make it possible to control diffusive fields according to human preference and will. Here, we theoretically establish a temperature-dependent transformation method for controlling multiphysics whose intrinsic physical parameters depend on temperature. Finite-element simulations demonstrate perfect thermoelectric cloaking, concentrating, and rotating performance. Two practical applications are designed with nonlinear transformation. One is an ambient-responsive cloak-concentrator device; the other is an improved thermoelectric cloak with simultaneous near-thermostat performance inside.

**Theory.** At a steady state with local equilibrium, the governing equations of TE transport are expressed as:

$$\nabla \cdot J = 0,$$

$$\nabla \cdot J_Q = -\nabla \mu \cdot J,$$

$$J = -\sigma(T) \cdot \nabla \mu - \sigma(T) S(T) \nabla T,$$

$$J_Q = -\kappa(T) \cdot \nabla T + T S^T(T) J.$$

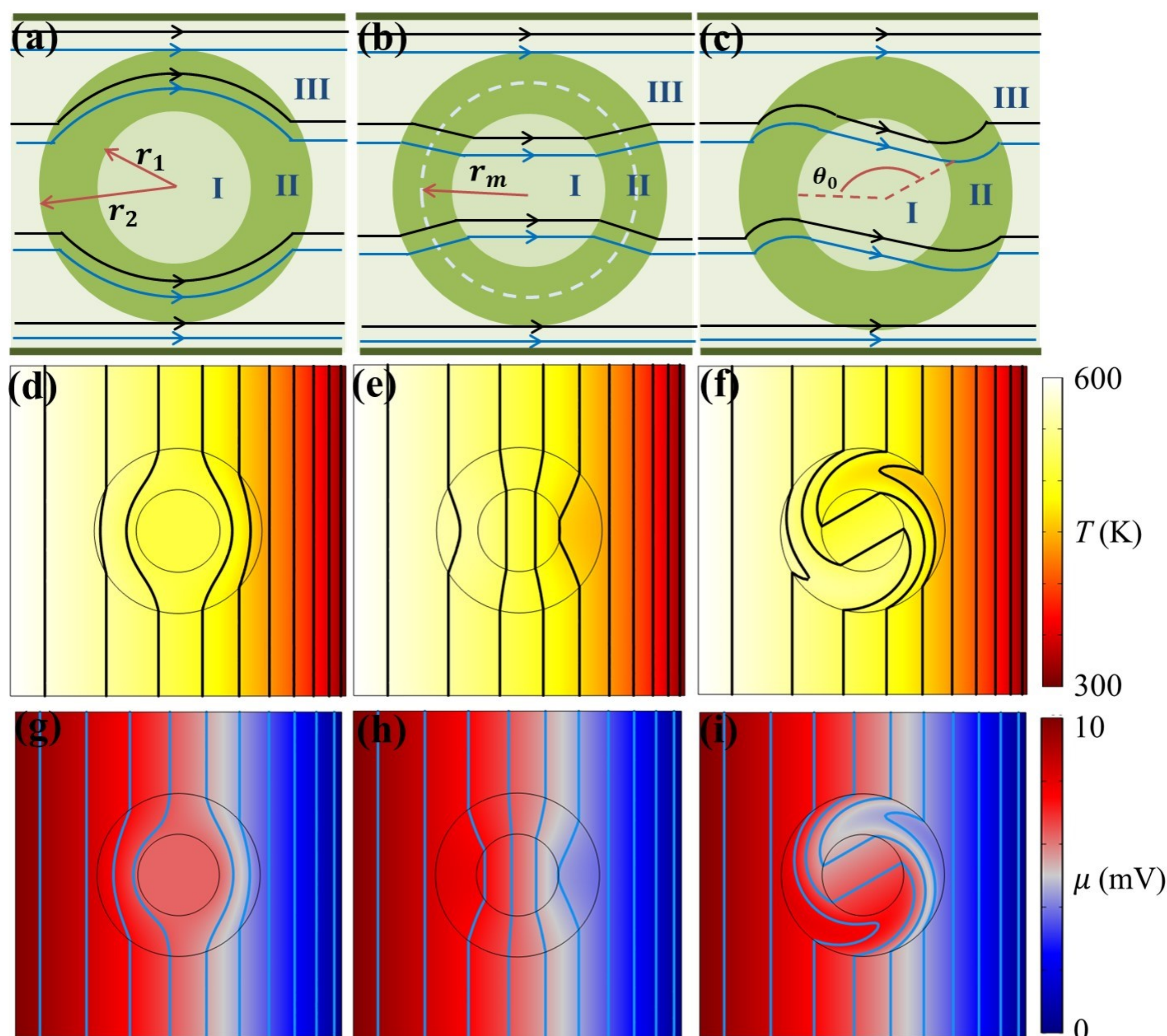
Using the temperature-dependent transformation theory for the thermoelectric control equation, considering the temperature-dependent material parameters, the transformed thermal conductivity, electrical conductivity and Seebeck coefficient can be written as:

$$\kappa'(T) = \frac{A \sigma(T) A^T}{\det A},$$

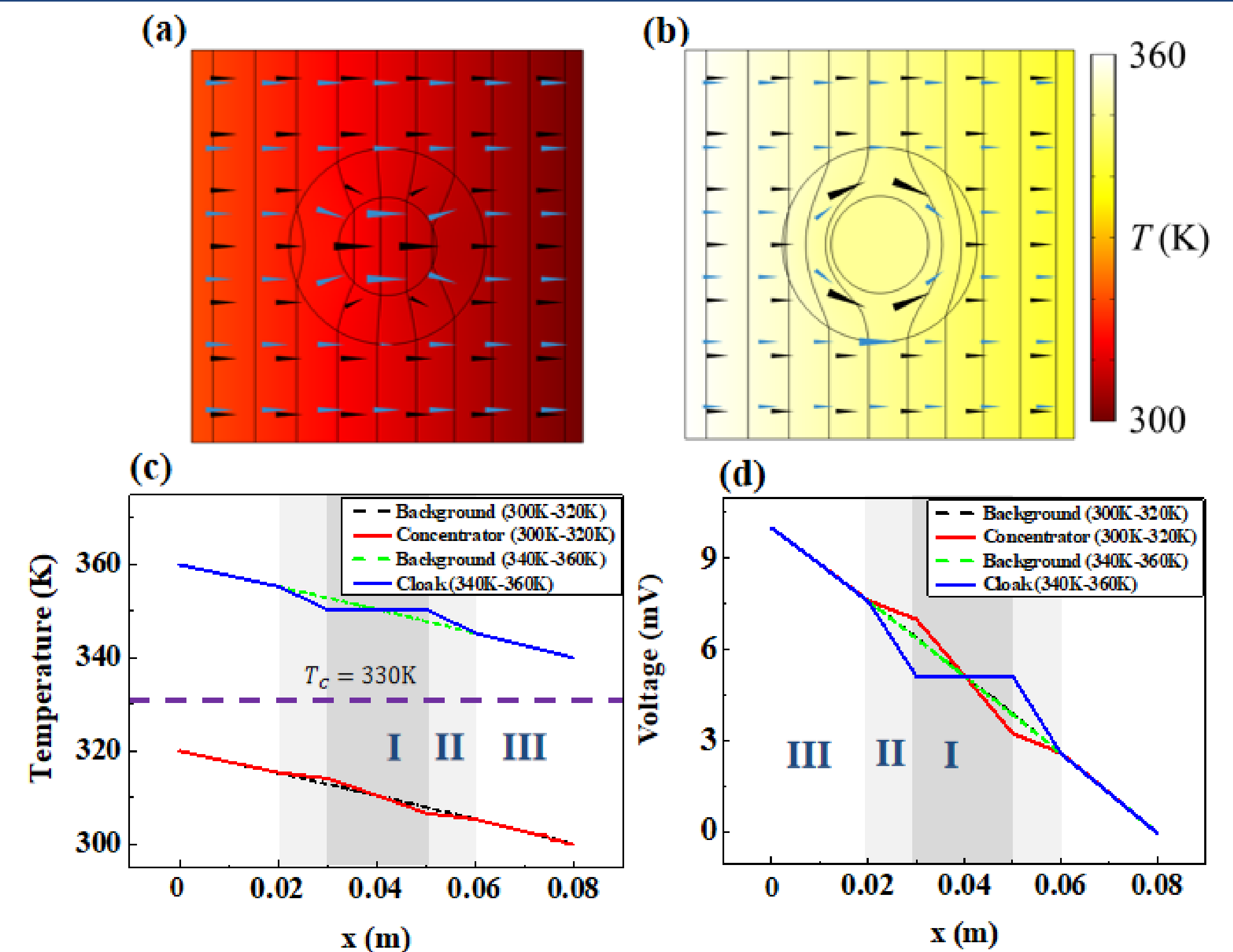
$$\sigma'(T) = \frac{A \kappa(T) A^T}{\det A},$$

$$S'(T) = A^{-T} S(T) A^T.$$

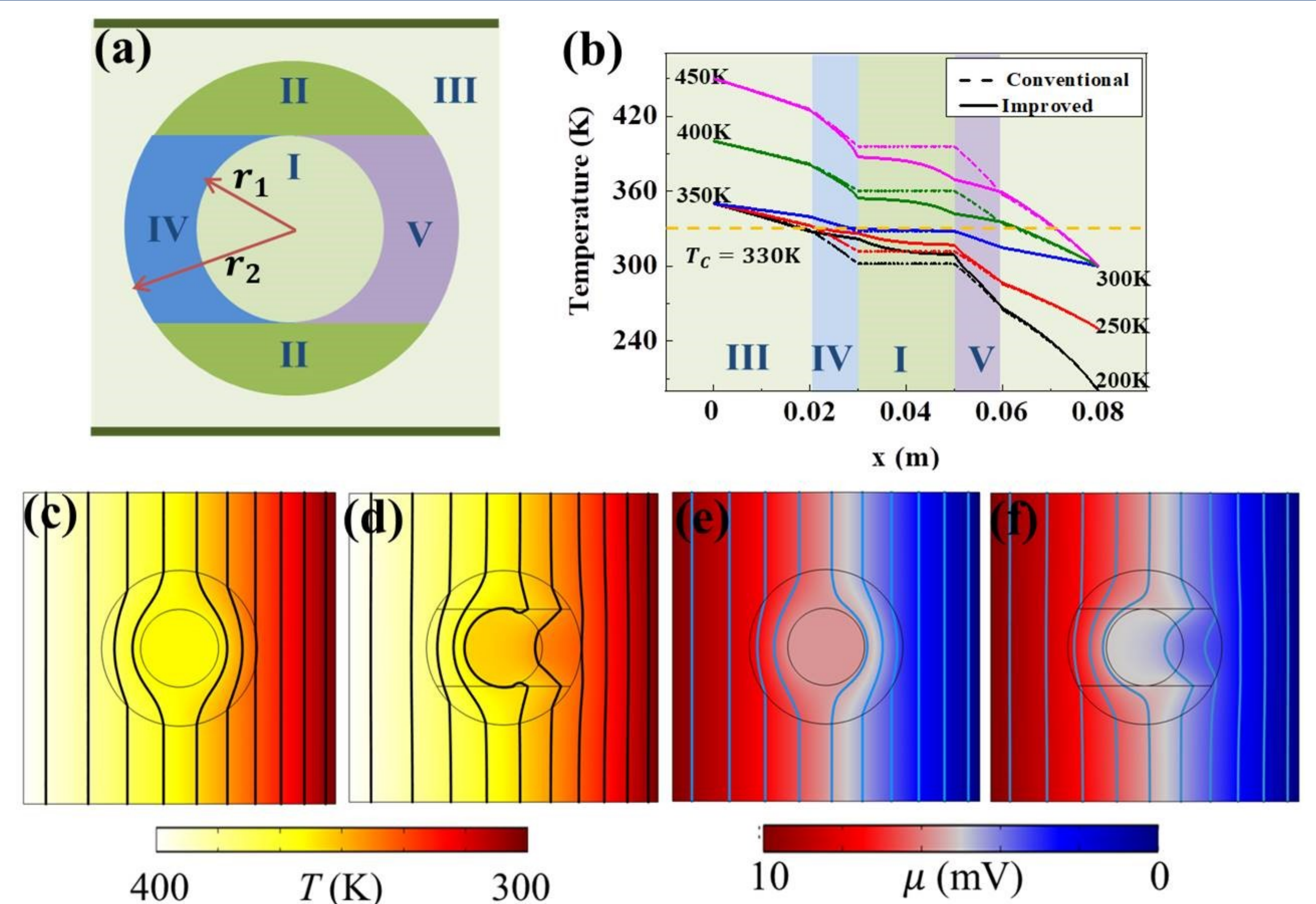
Based on these parameters, thermoelectric cloaks, concentrators, and rotators can be designed.



**Simulation-1.** The structure of thermoelectric cloak, concentrator, rotator are depicted in (a)-(c), simulation results are shown in (d)-(i). (d)-(f) Simulation results of temperature distribution, and (g)-(i) simulation results of potential distribution, corresponding to (a)-(c).



**Simulation-2.** Ambient-responsive cloak-concentrator. (a)-(b) Simulation results of the thermoelectric cloak-concentrator. (c) and (d) are the temperature and voltage curves of the center lines extracted from simulation results in (a) and (b).



**Simulation-3.** Improved thermoelectric cloak. (c)-(e) Temperature and potential distributions of a conventional thermoelectric cloak, respectively. (d)-(f) Temperature and potential distributions of the improved thermoelectric cloak.

## Conclusion.

1. Established temperature-dependent transformation thermoelectrics.
2. Designed temperature-dependent thermoelectric cloaks, concentrators, and rotators.
3. Designed two kinds of practical devices: ambient-responsive cloak-concentrator and improved thermoelectric cloak.