



# Topological bands in two-dimensional orbital-active bipartite lattices

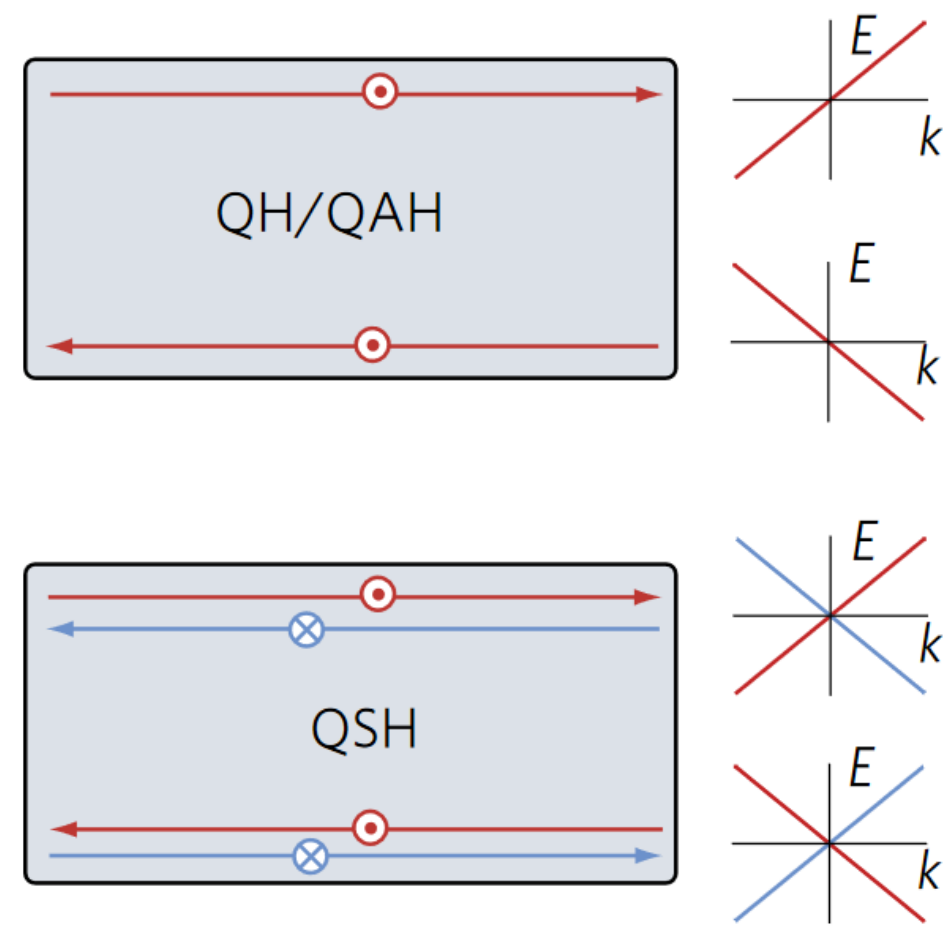
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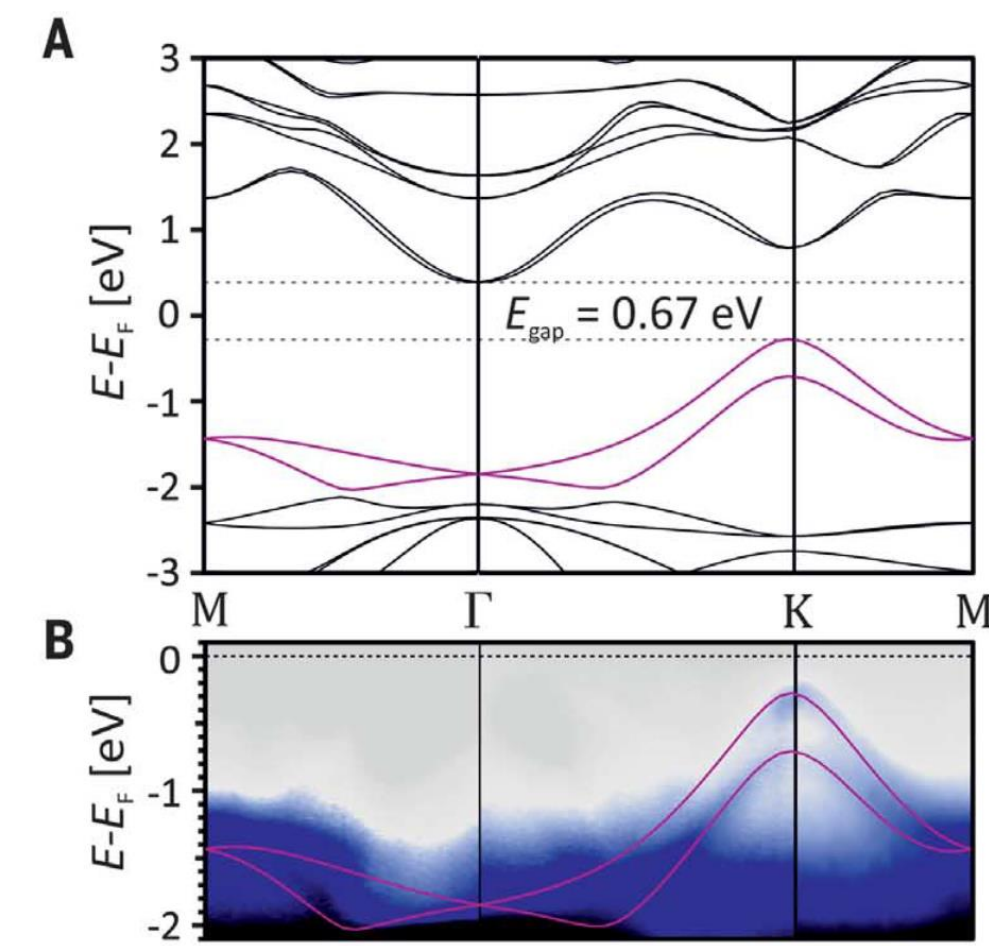
## Motivation

The search for large gap quantum spin Hall (QSH) and quantum anomalous Hall (QAH) insulators is important both for fundamental and practical interests.



The degenerate multi-orbitals  $p_x, p_y$  in honeycomb lattice provides a paradigm for QSH state with a boosted topological gap of the first order in atomic spin-orbit coupling.

Wang, J., Zhang, S.C. *Nature Mater* **16**, 1062–1067



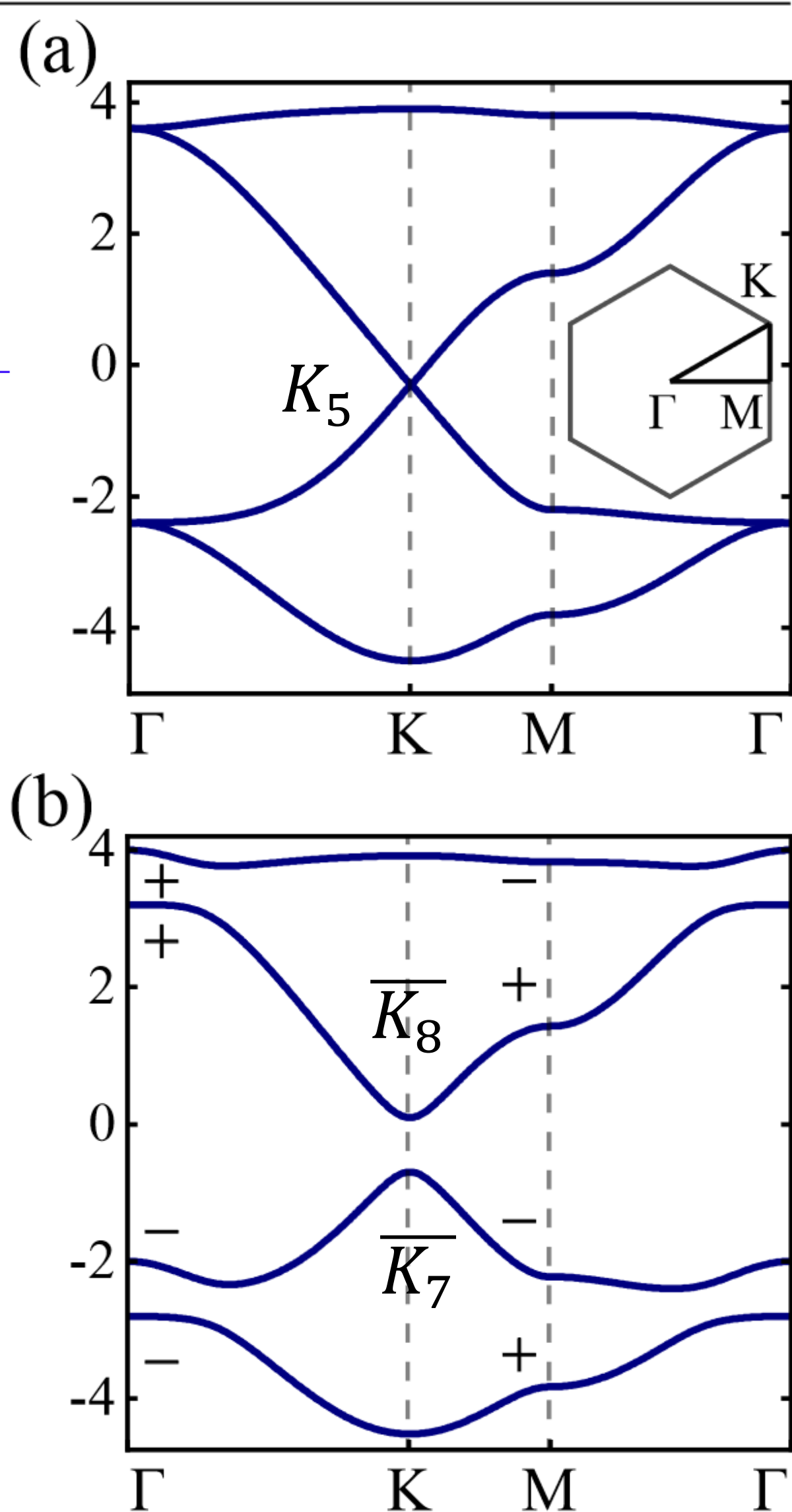
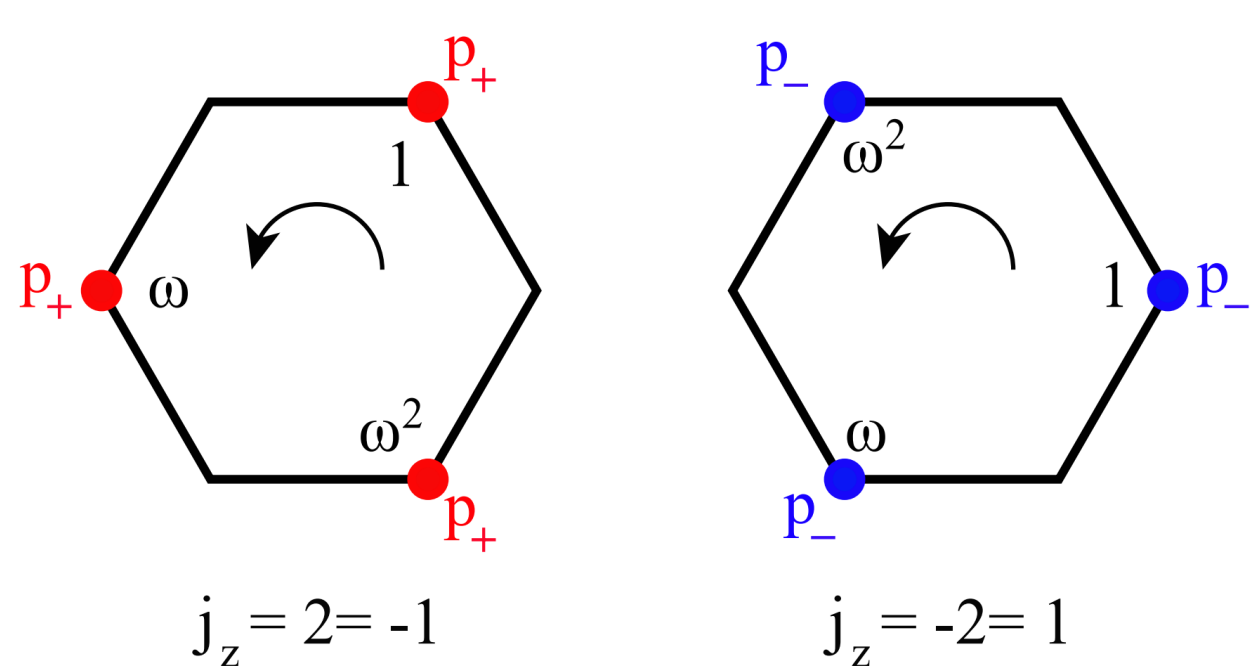
F. Reis, G. Li, et al, *Science* **357**, 287–290 (2017)

This motive us to explore the relation between symmetry and such large gap mechanism

## Method

Topological Quantum Chemistry (TQC)

spinless	$\Gamma$	$K$	$M$
$p_z$	$\Gamma_2^- \oplus \Gamma_3^+$	$K_6$	$M_2^- \oplus M_3^+$
$p_x p_y$	$\Gamma_5^+ \oplus \Gamma_6^-$	$K_5 \oplus K_1 \oplus K_4$	$M_1^+ \oplus M_2^+ \oplus M_3^- \oplus M_4^-$
spinful	$\Gamma$	$K$	$M$
$p_+^\uparrow p_-^\uparrow$	$\bar{\Gamma}_8^+ \oplus \bar{\Gamma}_{12}^-$	$\bar{K}_7 \oplus \bar{K}_9$	$\bar{M}_5^+ \oplus \bar{M}_6^-$
$p_+^\uparrow p_-^\downarrow$	$\bar{\Gamma}_7^+ \oplus \bar{\Gamma}_{10}^-$	$\bar{K}_8 \oplus \bar{K}_9$	$\bar{M}_5^+ \oplus \bar{M}_6^-$



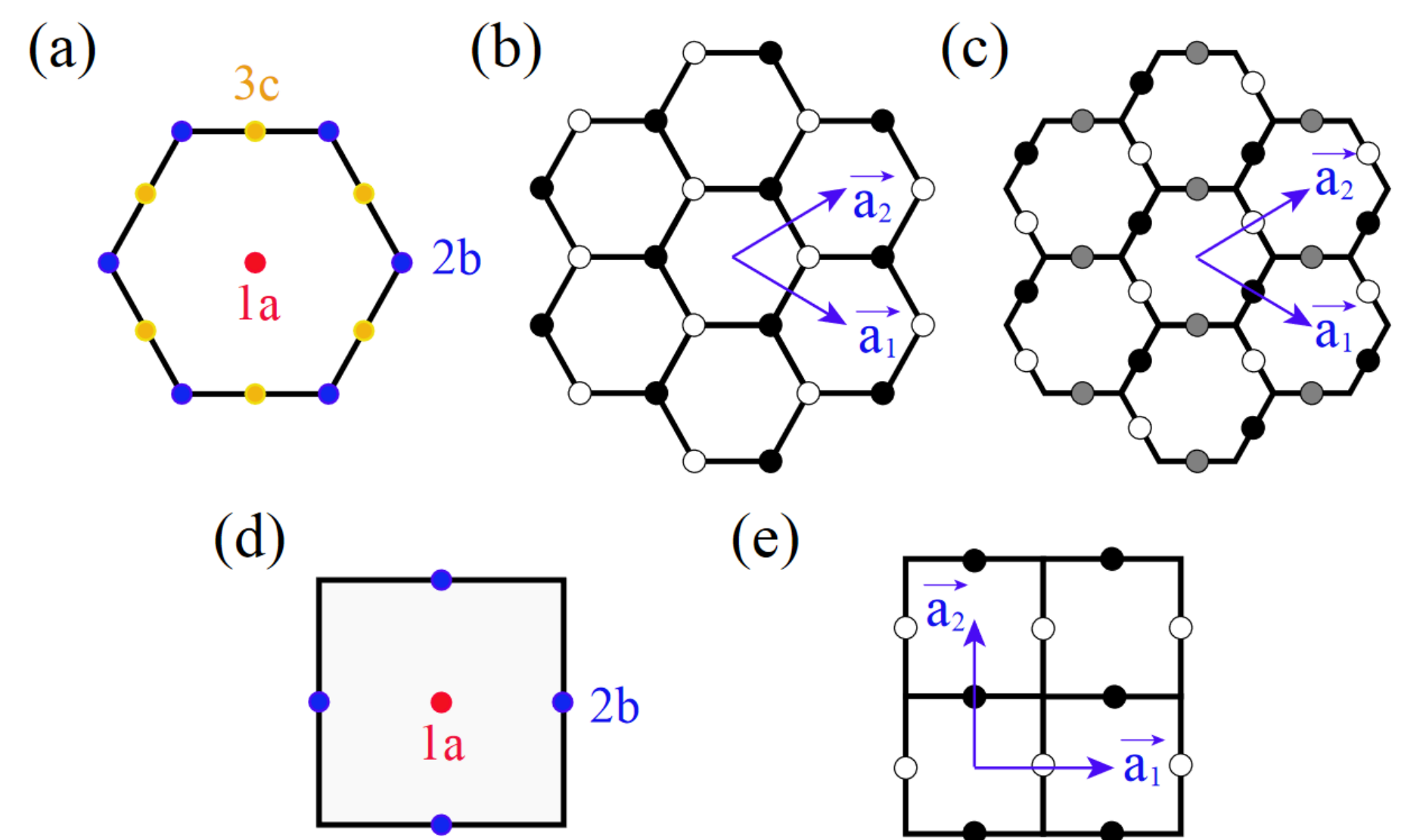
$$\vec{s} \cdot \vec{l}$$

$$p_+^\uparrow \Rightarrow \frac{\lambda_{soc}}{2} \quad p_+^\downarrow \Rightarrow -\frac{\lambda_{soc}}{2}$$

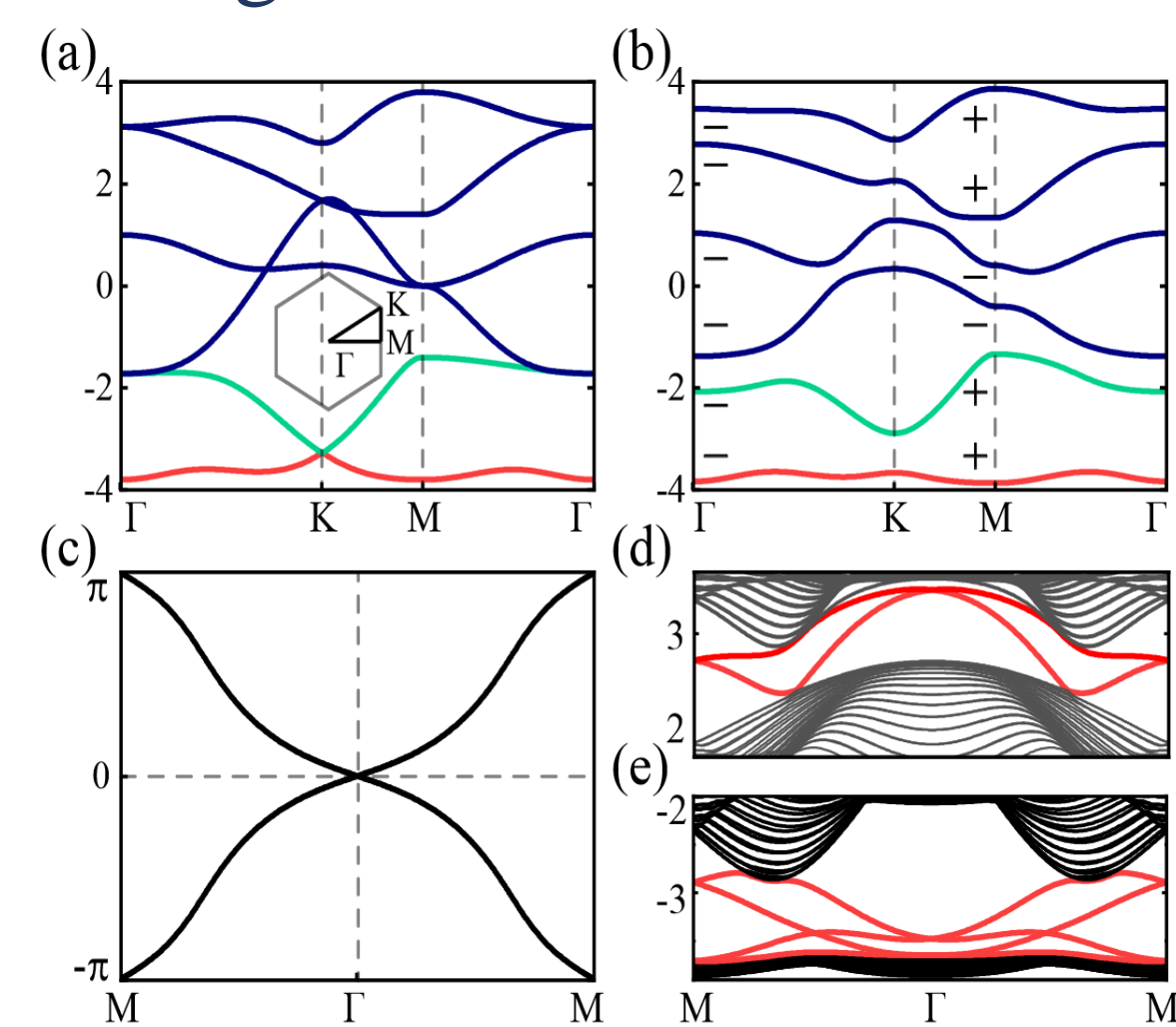
$$p_-^\downarrow \Rightarrow \frac{\lambda_{soc}}{2} \quad p_-^\uparrow \Rightarrow -\frac{\lambda_{soc}}{2}$$

$$j_z = \mp \frac{3}{2} \quad j_z = \mp \frac{1}{2}$$

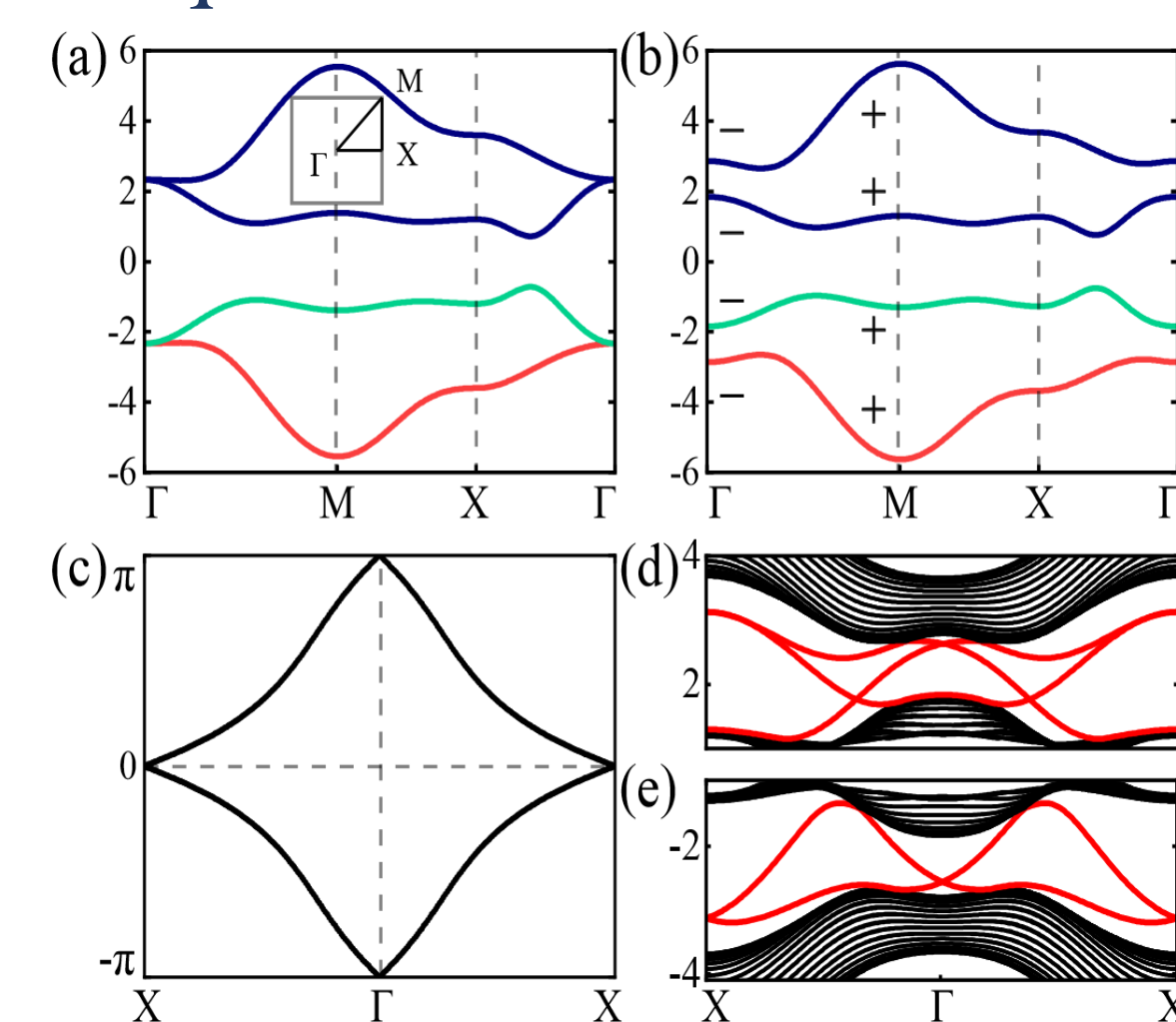
## Result



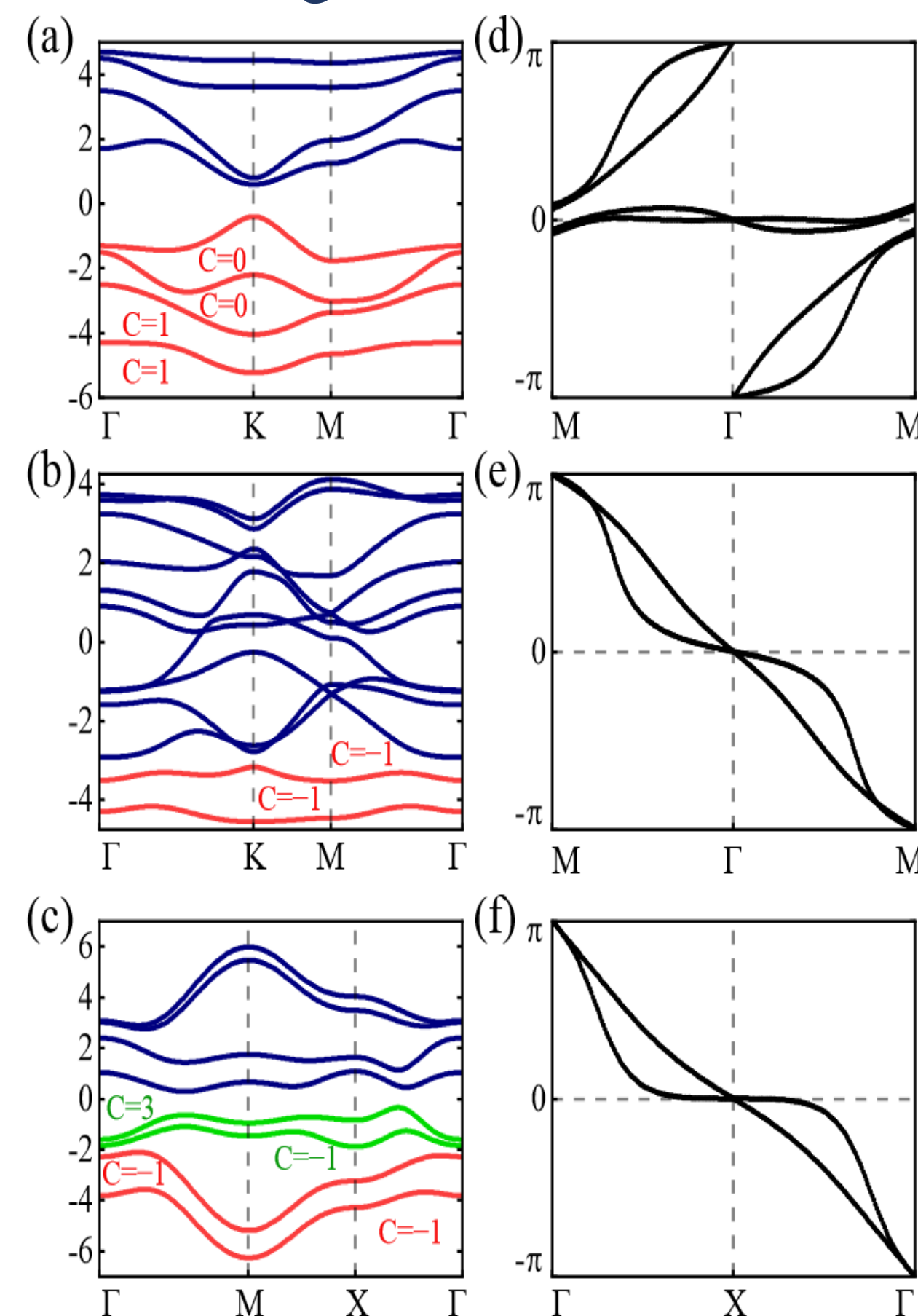
Kagome lattice



Square lattice



Add magnetism



## Summary

We extend the large gap QSH state on honeycomb lattice to general 2D lattices, which is based on symmetry analysis and EBRs, though we find such phenomenon in many other lattice, if we further consider the filling, honeycomb lattice is still the best case. On the other hand, it also explain why honeycomb lattice is the first discovered system to hold such mechanism.

## Reference

[1] B. Bradlyn, L. Elcoro, J. Cano, M. G. Vergniory, Z. Wang, C. Felser, M. I. Aroyo, and B. A. Bernevig, "Topological quantum chemistry," *Nature (London)* **547**, 298–305 (2017)

[2] Gu-Feng Zhang, Yi Li, and Congjun Wu, "Honey-comb lattice with multi-orbital structure: Topological and quantum anomalous hall insulators with large gaps," *Phys. Rev. B* **90**, 075114 (2014)

