Nanoscale Casimir force softening originated from surface electrons

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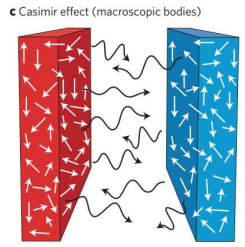
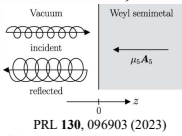
Abstract

Strong coupling between vacuum fields and quantum matter occurs at the nanoscale and broadens the horizon of light-matter interaction. Nanoscale Casimir force, as an exhibition of vacuum fields, inevitably experiences the influence of surface electrons due to their quantum character, which are ignorable in micron Casimir force. Here, we develop a three-dimensional conformal map method to tackle typical experimental configurations with surface electron contributions to Casimir force purposely and delicately included. Based on this method, we reveal that surface electrons can either enhance or suppress the nanoscale Casimir force, depending on materials and crystal facets. The mechanism is demonstrated to be the Casimir force softening, which results from surface electrons effectively altering the distance seen by the Casimir interaction. Our findings not only highlight the interaction between surface electrons and vacuum fields but also provide a recipe for theoretical and experimental investigation of nanoscale fluctuation-type problems.

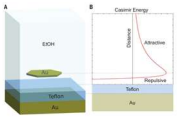
Background: Casimir effect, strong coupling, surface electrons



A review: Nat. Photon. **5**, 211 (2011)



PRL **130**, 096903 (2023)

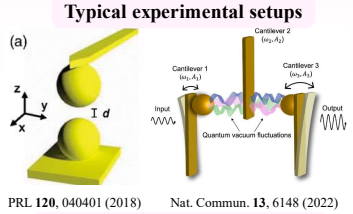


Science **364**, 984 (2019)

Science **375**, 1030 (2022)

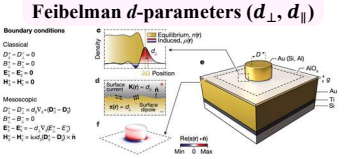
Science **373**, 178 (2021)

Typical experimental setups



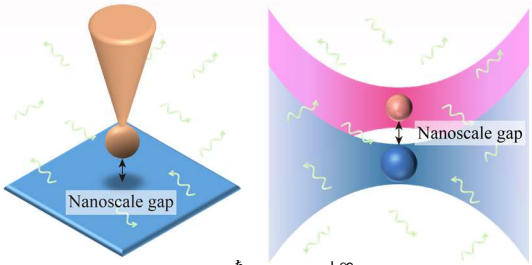
PRL **120**, 040401 (2018) Nat. Commun. **13**, 6148 (2022)

Feibelman d-parameters ($d_\perp$, $d_\parallel$)



Nature **576**, 248 (2019)

Motivation: *Nanoscale Casimir Force?*

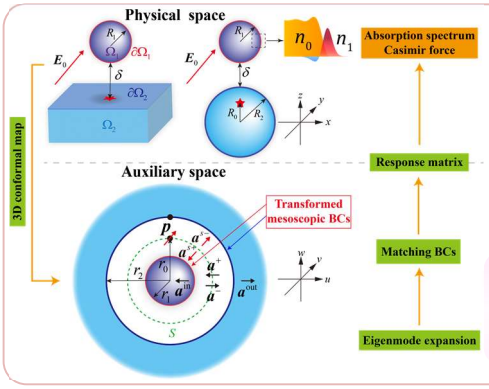


Casimir formula: $E = \frac{\hbar}{4\pi}\sum_{m=0}^{+\infty}\int_{-\infty}^{+\infty} \ln f_m(\omega = i\xi)\,\mathrm{d}\xi$

Challenges: **Scattering matrix** of all EM modes (to obtain $\boldsymbol{f_m}$)

- Handle such **experimental structures** (not only planes)
- Include the response of **surface electrons** (beyond ε and μ)
- Require calculations to be **reliable** and **efficient** (all ω and k)

3D-CM Method



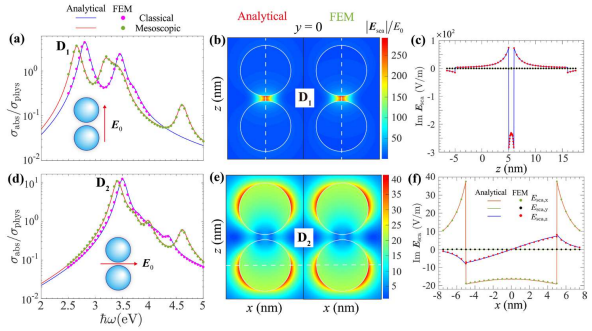
Response matrix equation

$$\mathbf{S}_{m,\mathrm{wd}}\begin{pmatrix}\boldsymbol{a}_m^+\\ \boldsymbol{a}_m^-\end{pmatrix}=\begin{pmatrix}\boldsymbol{a}_m^{s+}\\ \boldsymbol{a}_m^{s-}\end{pmatrix},$$

$$\mathbf{S}_{m,\mathrm{wd}}=\begin{pmatrix}-\mathbf{I} & \mathbf{S}_{m,\mathrm{wd}}^{++}{}^{-1}\mathbf{T}_{m,\mathrm{wd}}^{+-}\\ \mathbf{S}_{m,\mathrm{wd}}^{--}{}^{-1}\mathbf{T}_{m,\mathrm{wd}}^{-+} & -\mathbf{I}\end{pmatrix}$$

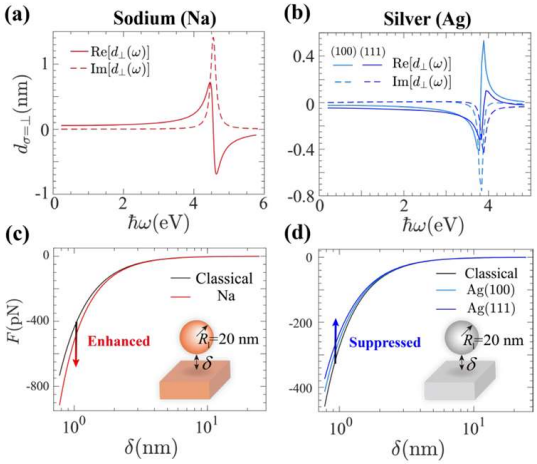
- **Key**: transform mesoscopic BCs to the auxiliary space.
- Obtain scatterings of full EM waves **efficiently** and **accurately**.

Benchmark: absorption spectrum and field profiles

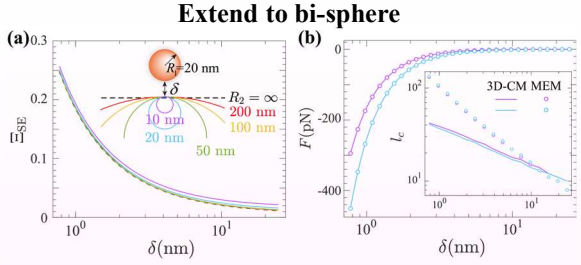


Nanoscale Casimir force: softening

Enhancement/suppression of Casimir force

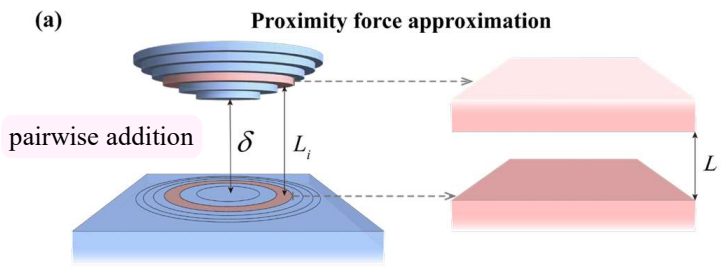


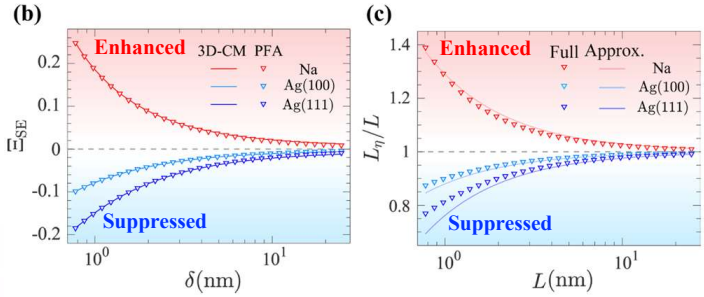
Extend to bi-sphere



- **MEM:** multipole expansion method

Casimir softening under PFA





Surface electron correction factor: $\Xi_{\mathrm{SE}} = \frac{F_{\mathrm{wd}}}{F_{\mathrm{cl}}} - 1$

Classical **reduction factor**: $\eta_F = \frac{F_{\mathrm{m}}}{F_{\mathrm{PEC}}} = \alpha_0\frac{L}{\lambda_p},\ \alpha_0 = 1.193,\ L \ll \lambda_p$

- In the nanoscale, $\boldsymbol{L \to L_\eta}$: nanoscale Casimir force softening distance [the *Full* markers]
- Assume that d_σ is weakly dispersive and $d_\sigma \ll L$, $\boldsymbol{L_\eta}$ is [*Approx.* lines]
  $\boldsymbol{L_\eta = L + \Sigma}$, $\boldsymbol{\Sigma = C_\perp d_\perp(i\xi=0) + C_\parallel d_\parallel(i\xi=0)}$, $\boldsymbol{C_\sigma}$**:** determined by **ε** and **>0**
- $\boldsymbol{\Sigma}$ only depends on $d_\perp$ and $d_\parallel$
- $\boldsymbol{d_\perp}$: centroid of induced surface electrons; $\boldsymbol{d_\parallel}$: total surface electrons

Conclusions

- ✓ A three-dimensional conformal map (3D-CM) method can handle **typical experimental geometries**, such as sphere-plate and bi-sphere.
- ✓ Our 3D-CM method is **efficient** and **accurate** whether it is compared with FEM or MEM.
- ✓ **Enhancement/suppression** of nanoscale Casimir force.
- ✓ Casimir **softening** distance $L_\eta = L + \Sigma$.

Hewan Zhang and Kun Ding†, arXiv:2403.11849