

X-RAY PHOTOGRAPHY

- Analyze **Laue diagram** of LiF monocrystal
- Investigate unknown powder samples using **Debye-Scherrer photograph**


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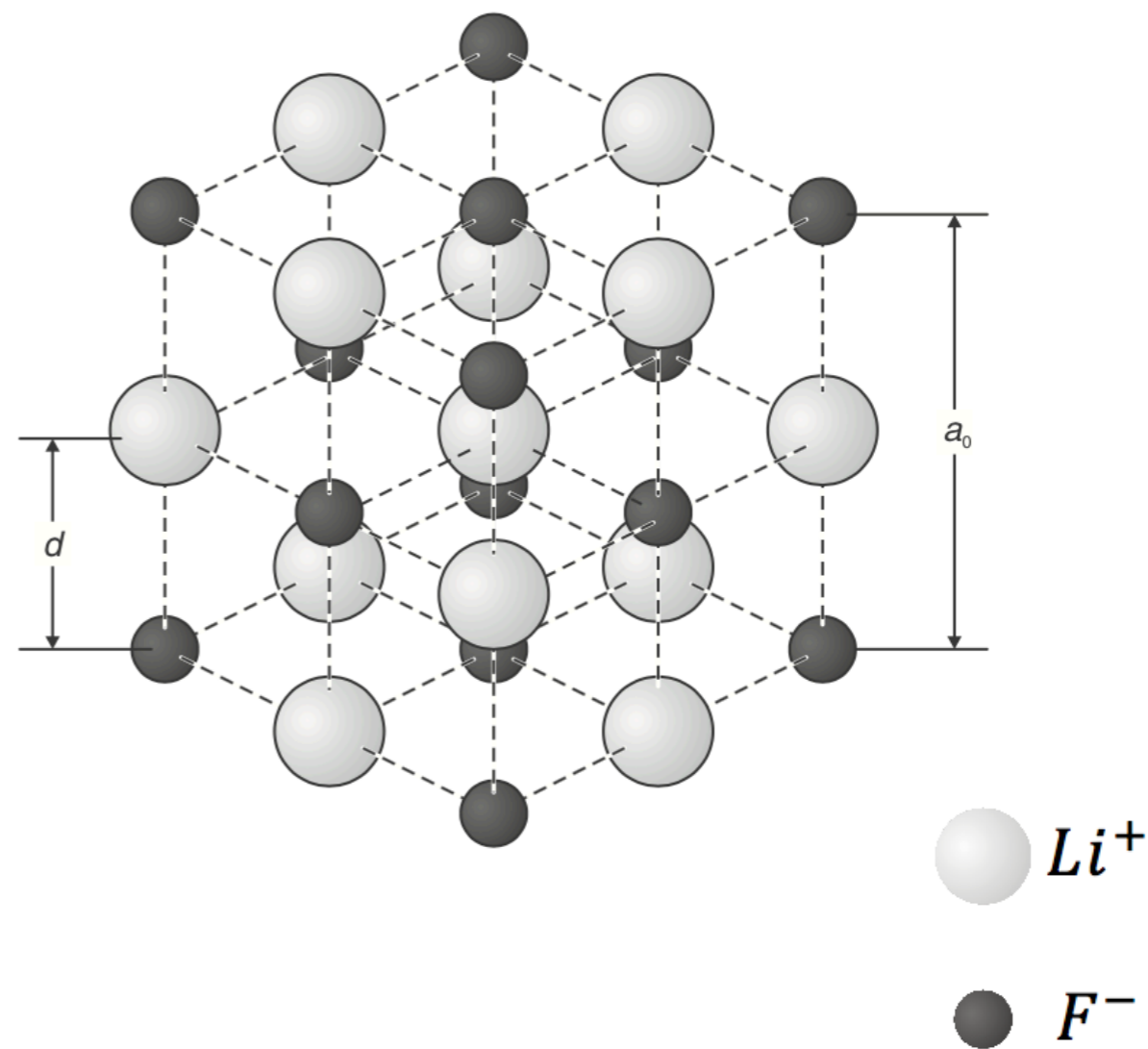
LiF Monocrystal



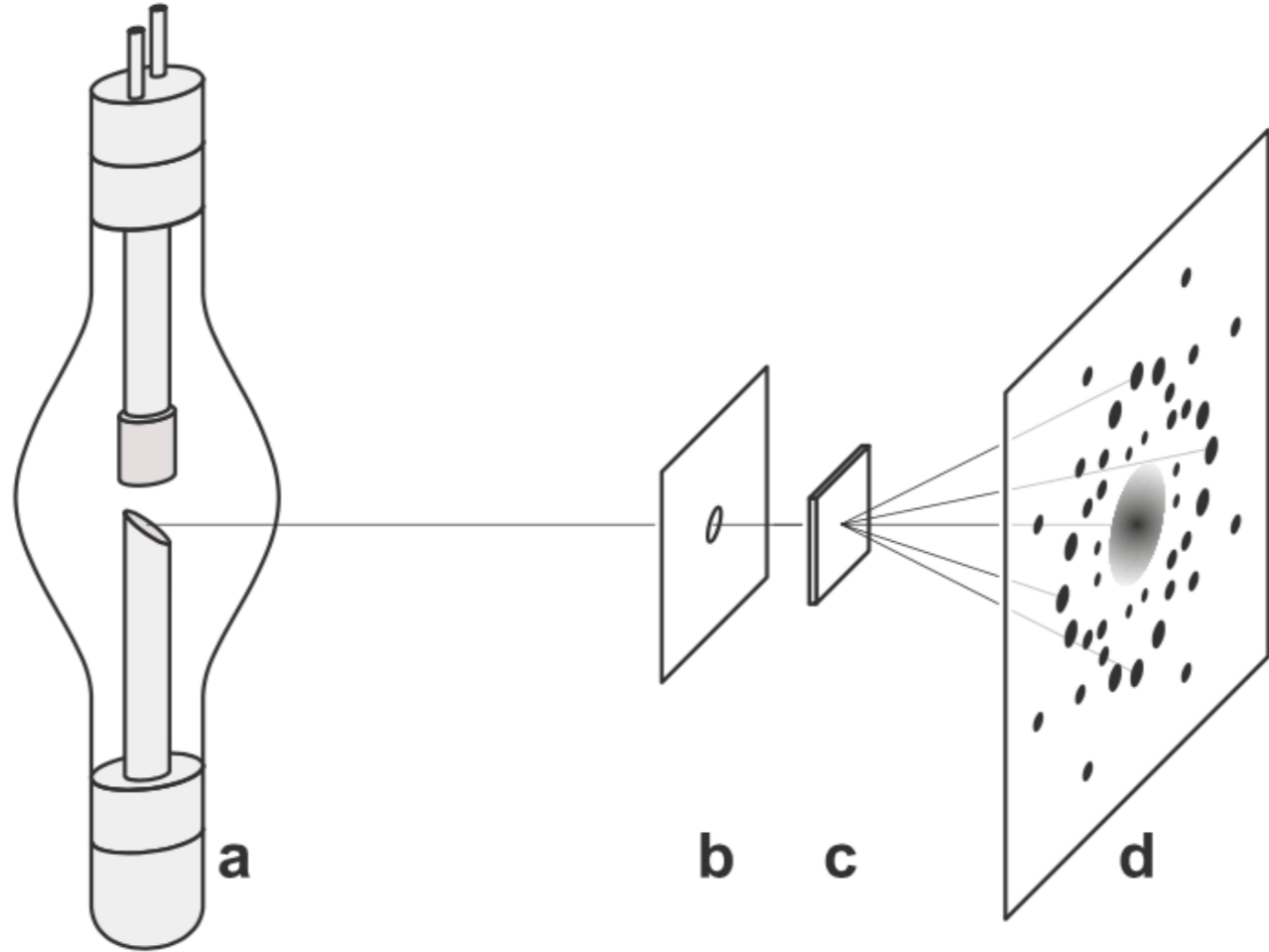
55477 LiF Crystal for Bragg Reflection

\$556.00

 Add to Cart



Laue Diagram



a
X-ray tube

b
Collimator

c
LiF Crystal

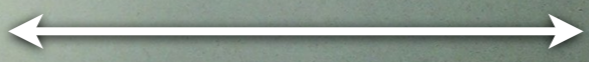
d
X-ray film

Collimator

LiF

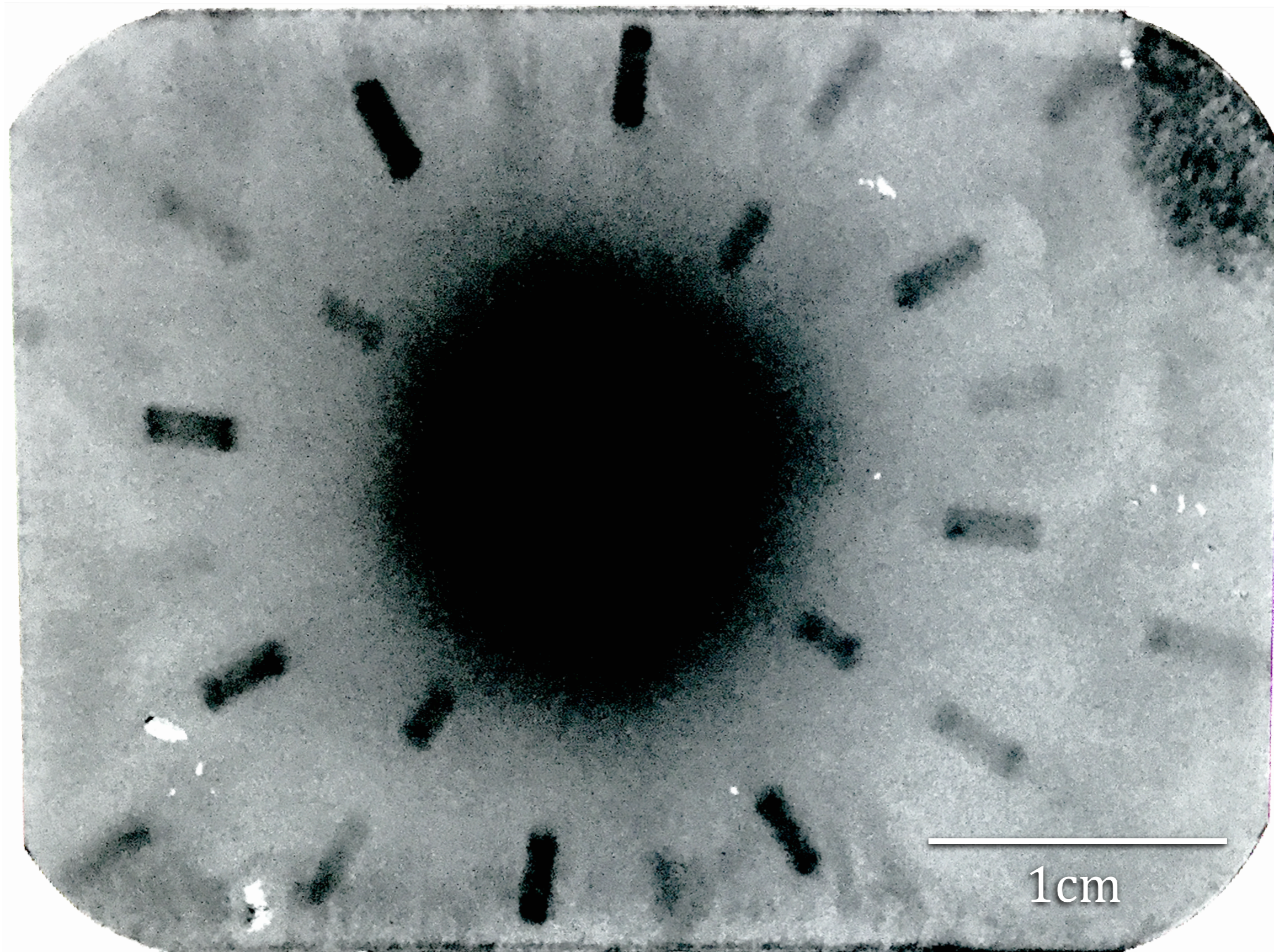
L

Film



GM-TUBE
INTERNAL RATEMETER





$L = 18\text{mm}$ *Time* = 1.5h Thickness = 5mm

$D_{\text{测}}$ (mm)

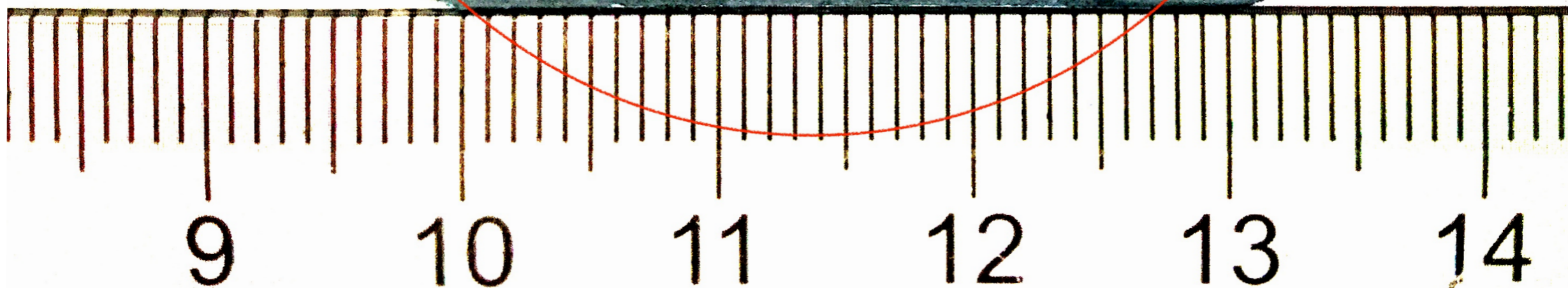
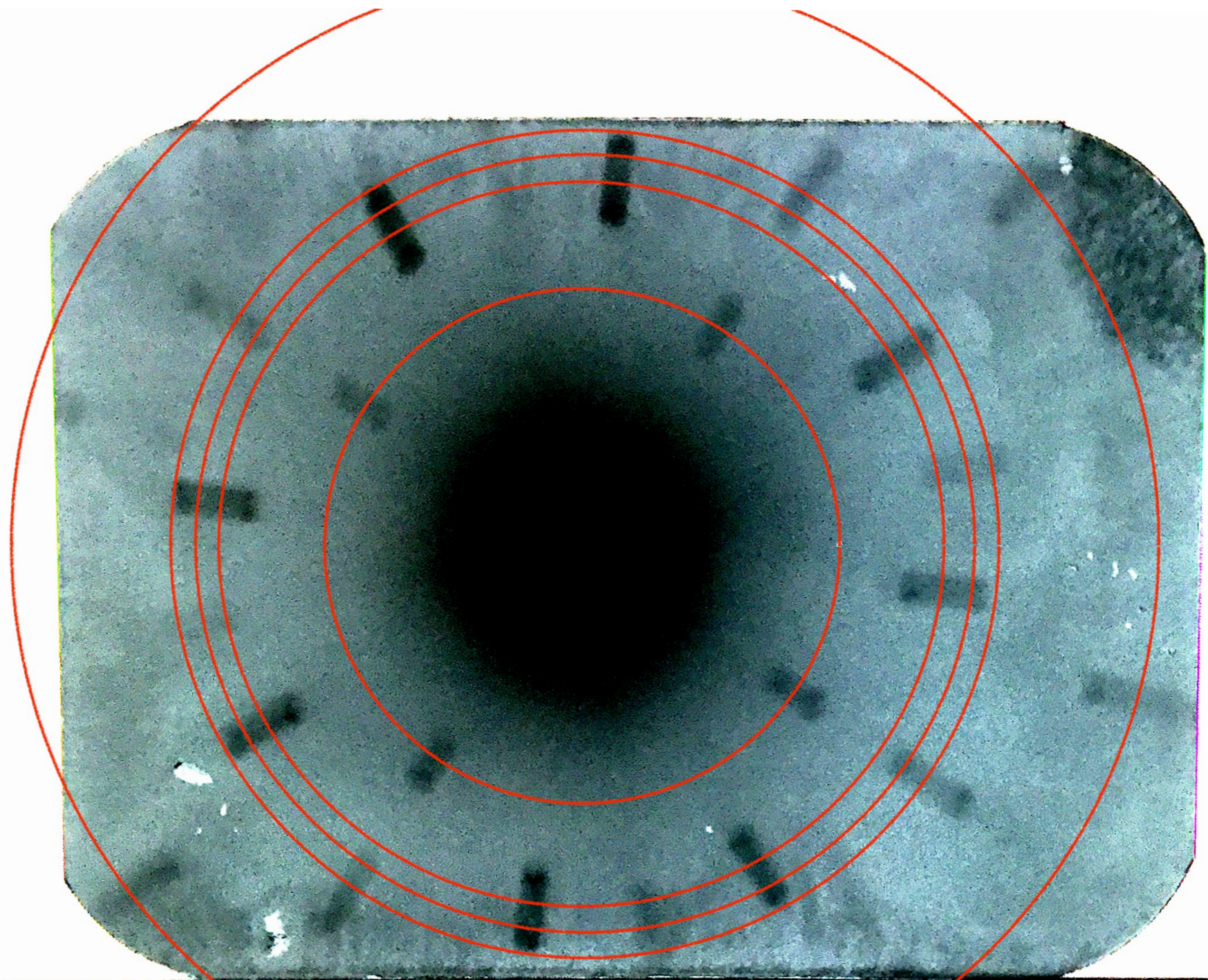
41.4

30.0

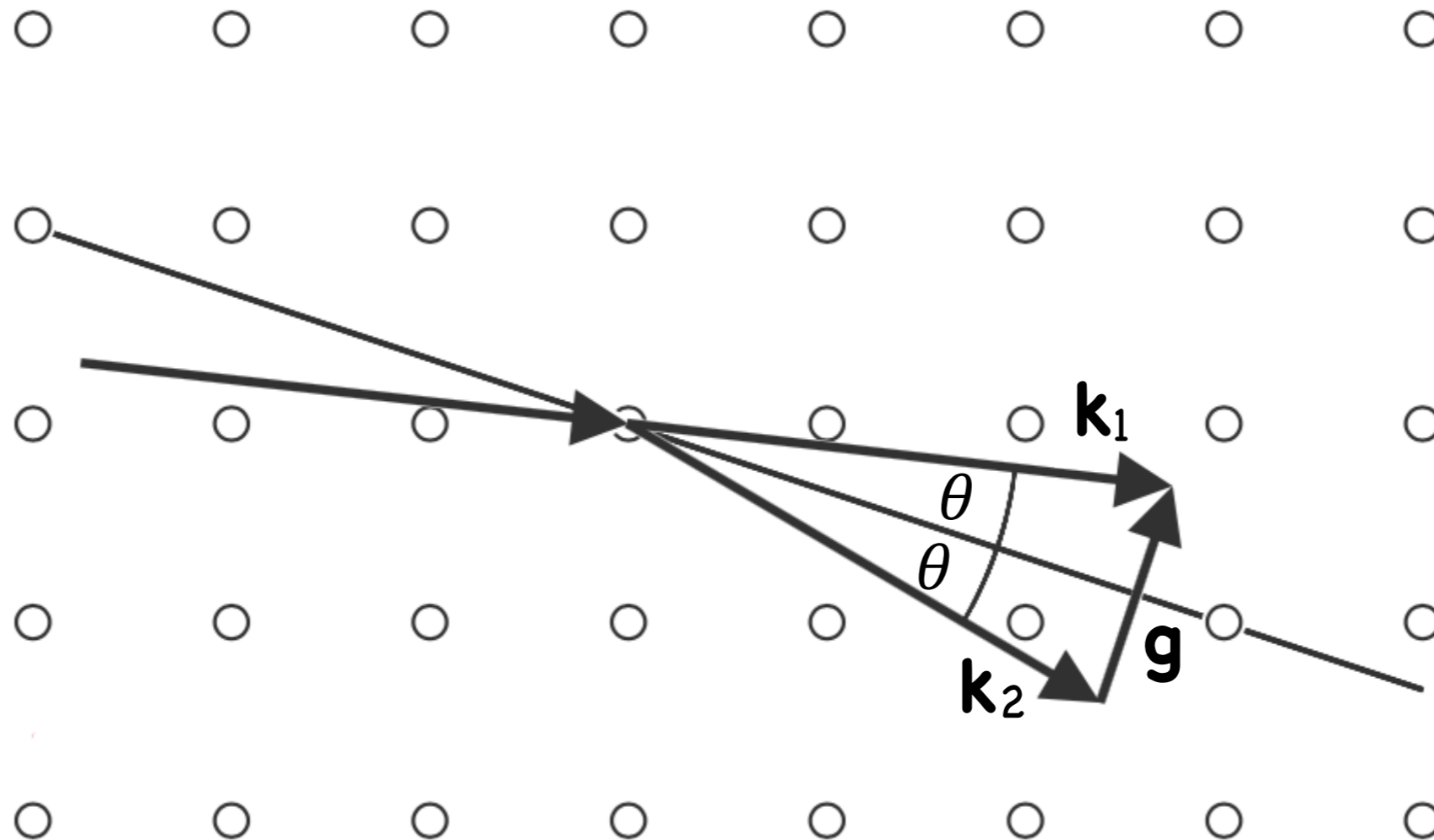
28.0

26.2

18.6



Laue Condition



$$k_1 - k_2 = g$$

$$|g| = 2|k| \sin \theta$$

$$\mathbf{g} = \frac{2\pi}{a_0} (h, k, l)$$

$$\sin \theta = \frac{l}{\sqrt{h^2 + k^2 + l^2}}$$

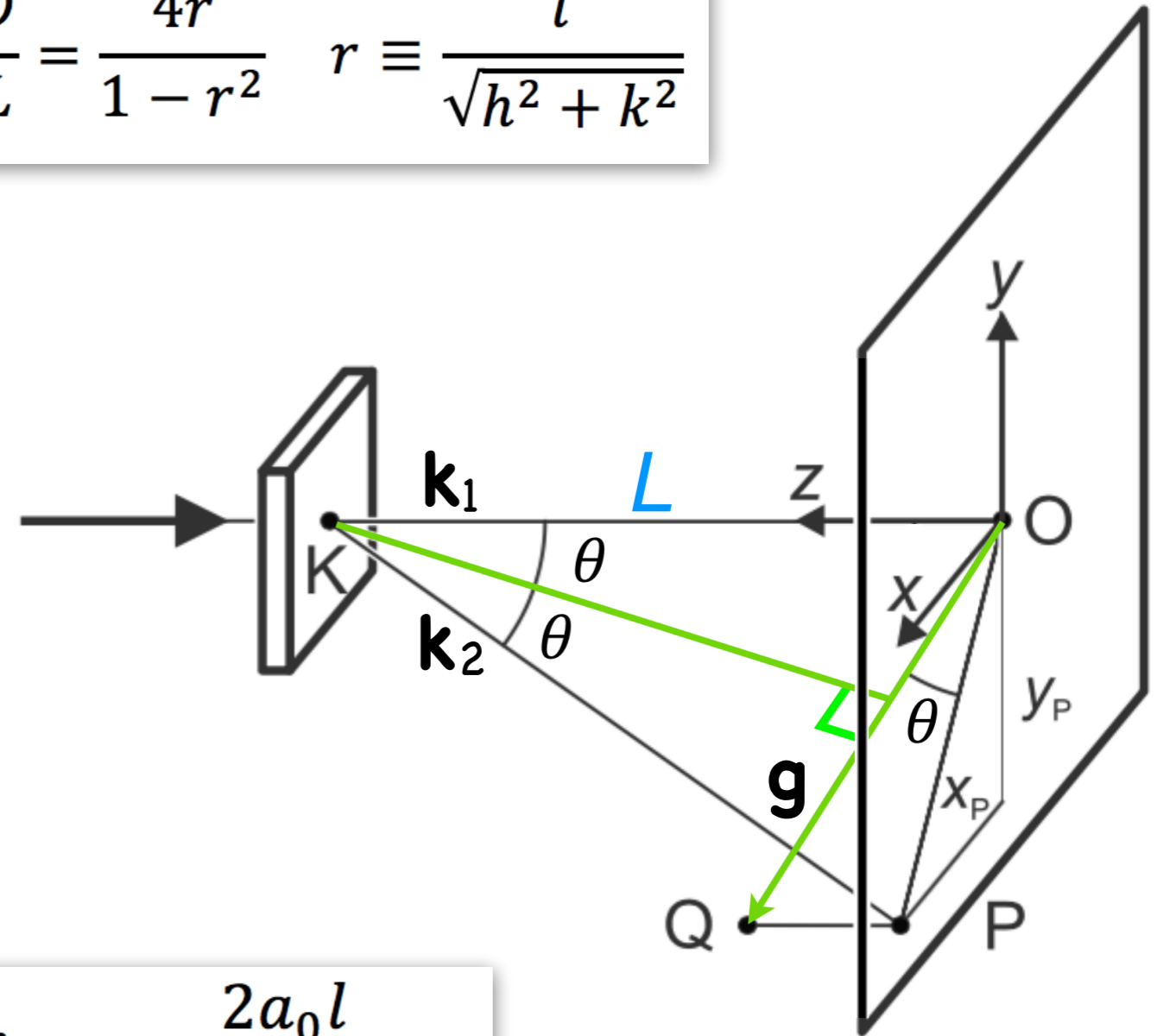
$$\tan 2\theta = \frac{\sqrt{x_p^2 + y_p^2}}{L} = \frac{D}{2L}$$

$$|\mathbf{g}| = 2|\mathbf{k}| \sin \theta$$

$$|\mathbf{g}| = \frac{2\pi}{a_0} \sqrt{h^2 + k^2 + l^2}$$

$$|\mathbf{k}| = \frac{2\pi}{\lambda}$$

$$\frac{D}{L} = \frac{4r}{1-r^2} \quad r \equiv \frac{l}{\sqrt{h^2 + k^2}}$$



$$\lambda = \frac{2a_0 l}{h^2 + k^2 + l^2}$$

$L = 18\text{mm}$



$D_{\text{测}}(\text{mm})$

41.4

30.0

28.0

26.2

18.6

$$\frac{4}{5} < \frac{D}{L} < 3$$

$$\frac{D}{L} = \frac{4r}{1 - r^2}$$

$$r \equiv \frac{l}{\sqrt{h^2 + k^2}}$$

$$4 < \frac{h^2 + k^2}{l^2} < 30$$

9

10

11

12

13

14

15

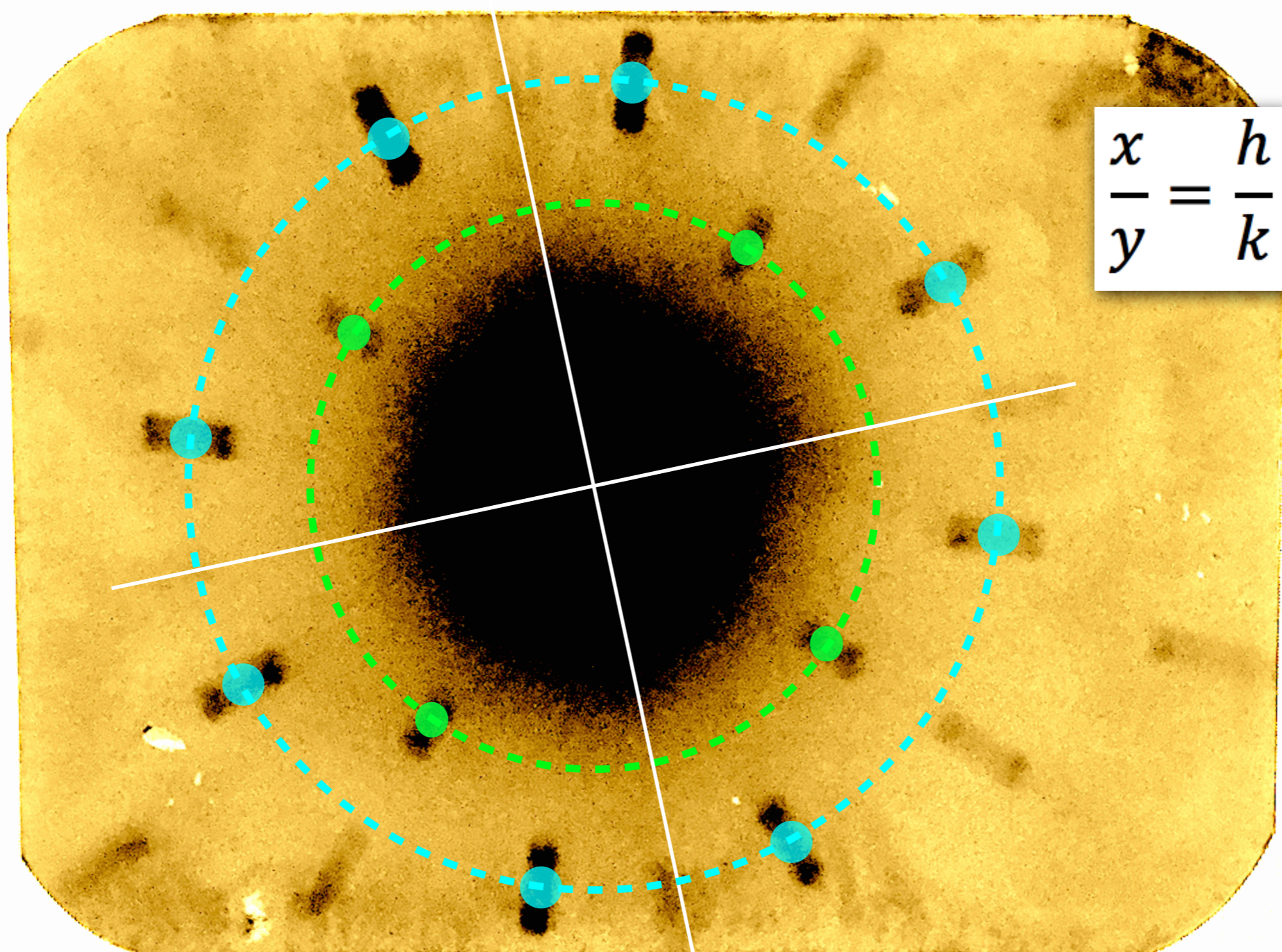
$$4 < \frac{h^2 + k^2}{l^2} < 30$$

h, k, l all even\odd.

$$\frac{D}{L} = \frac{4r}{1 - r^2} \quad r \equiv \frac{l}{\sqrt{h^2 + k^2}}$$

$$L_{\text{测}} = 18 \pm 1\text{mm} \quad u(D) = 0.2\text{mm}$$

multiplicity	h	k	l	D/L	$D_{\text{理论}}(\text{mm})$	$D_{\text{测}}(\text{mm})$	$L_{\text{理论}}(\text{mm})$
8	4	2	2	2.236	40.2	41.4	18.5
4	4	4	2	1.616	29.1	30.0	18.6
4	6	0	2	1.500	27.0	28.0	18.7
8	6	2	2	1.405	25.3	26.2	18.6
4	3	3	1	0.998	18.0	18.6	18.6
4	6	6	2				
8	8	2	2	1.031	18.6	-	-
8	8	4	2	0.942	17.0	-	-
8	8	6	2	0.833	15.0	-	-
8	5	1	1	0.816	14.7	-	-



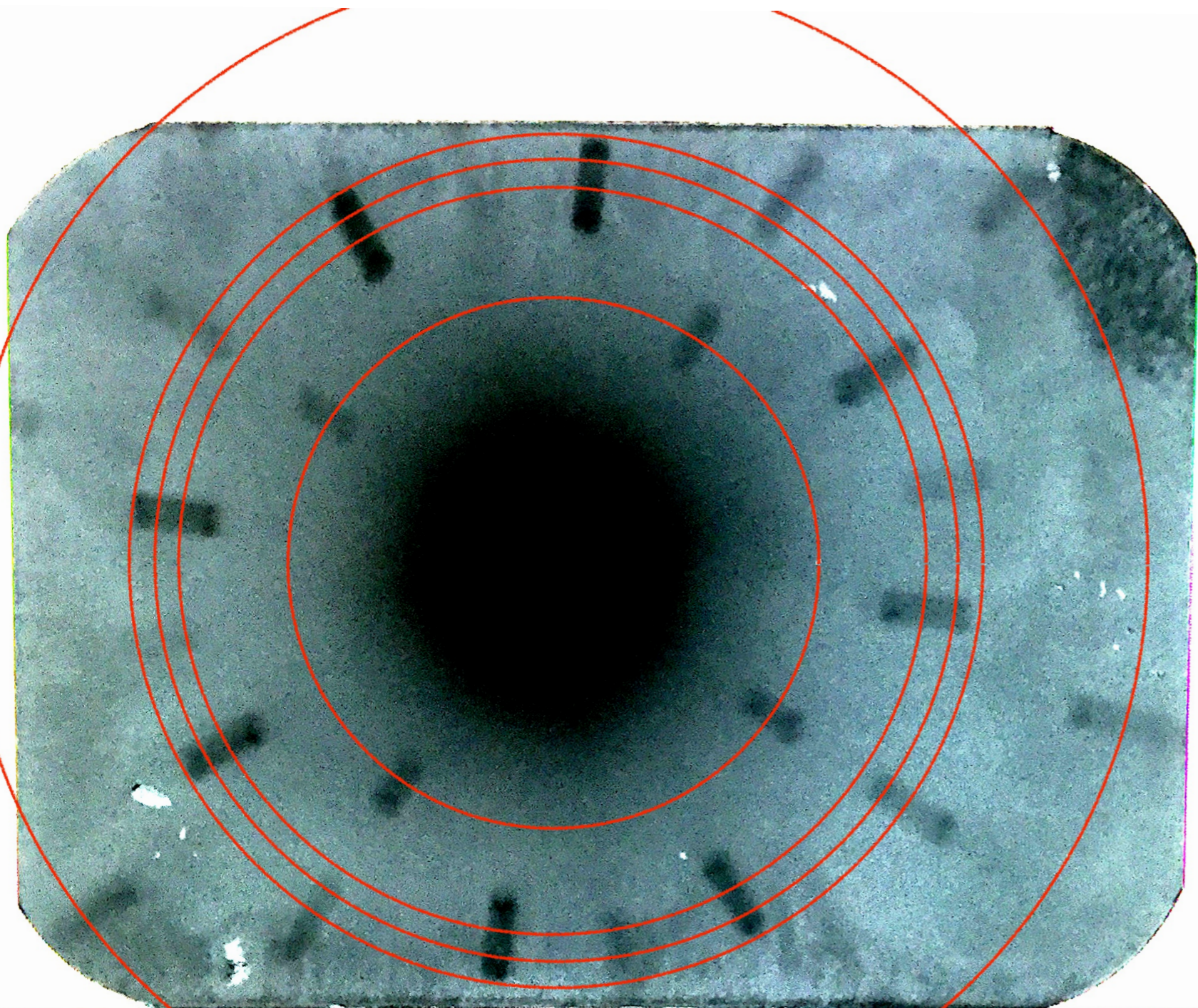
$$\frac{x}{y} = \frac{h}{k}$$

multiplicity	h	k	l	D/L	$D_{\text{理论}}(\text{mm})$	$D_{\text{测}}(\text{mm})$
8	6	2	2	1.405	25.3	26.2
4	3	3	1	0.998	18.0	18.6
4	6	6	2			
8	8	2	2	1.031	18.6	-
8	8	4	2	0.942	17.0	-

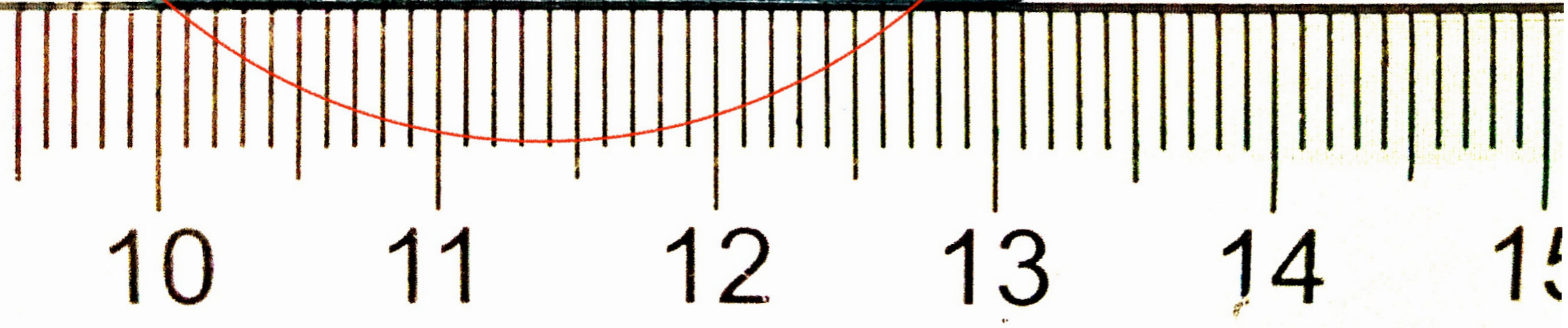
$$\lambda = \frac{2a_0l}{h^2 + k^2 + l^2}$$

$$U = 35\text{kV} \quad \lambda_{\min} = \frac{hc}{eU} = 35.43\text{pm}$$

h	k	l	D/L	D/mm	λ/pm
4	2	2	2.236	41.4	67.13
4	4	2	1.616	30.0	47.76
6	0	2	1.500	28.0	40.28
6	2	2	1.405	26.2	36.62
3	3	1	0.998	18.6	42.40
6	6	2			21.20
8	2	2	1.031	-	22.34
8	4	2	0.942	-	19.18
8	6	2	0.833	-	15.49
5	1	1	0.816	-	29.84



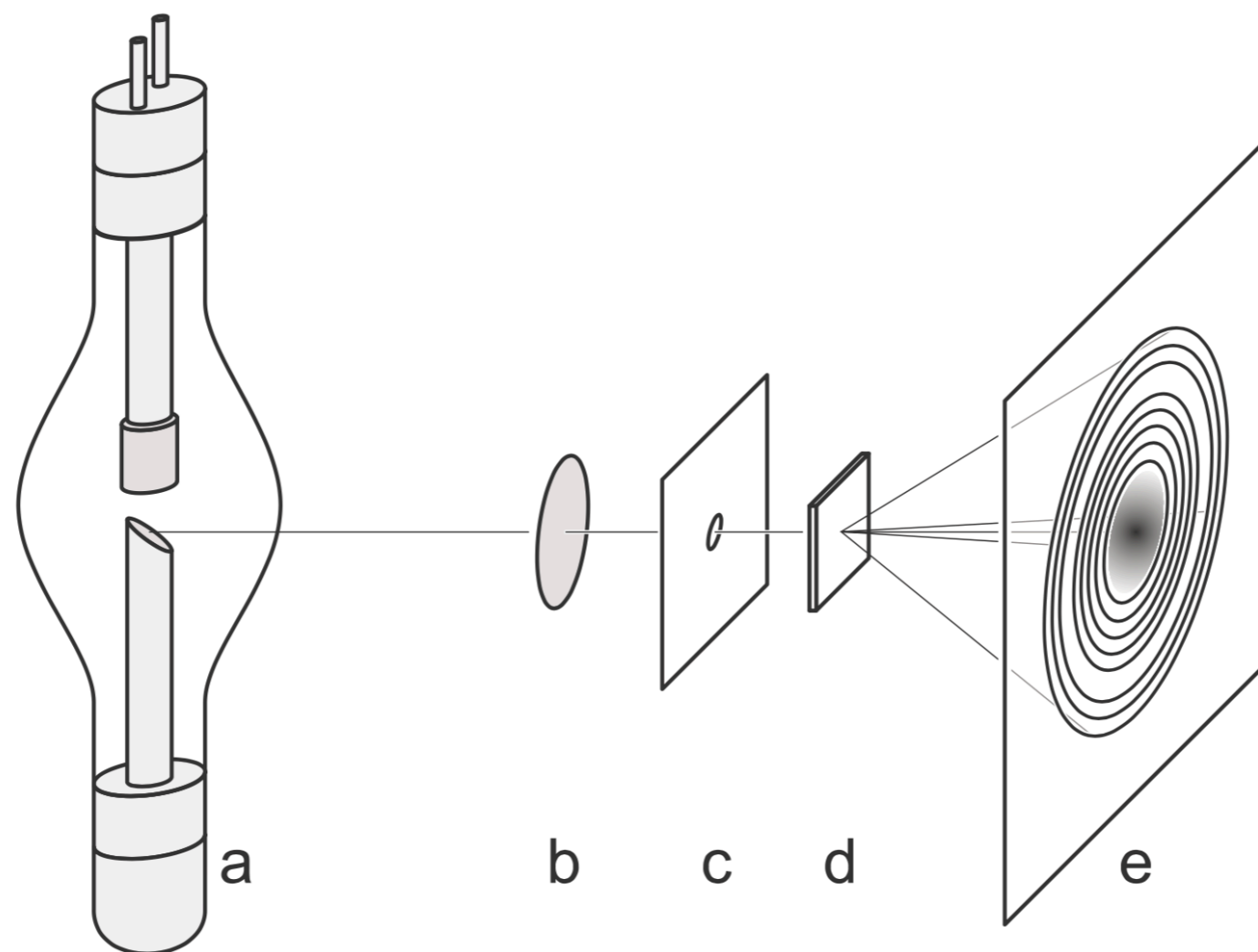
D/mm	$\{hkl\}$	λ/pm
41.4	422	67.13
30.0	442	47.76
28.0	602	40.28
26.2	622	36.62
18.6	331	42.40



References

- Simon, S. H. (2013)
The Oxford solid state basics. Chapter 14.
OUP Oxford.
- Leybold-Didactic. (2015)
Leybold Physics Leaflets. P 7.1.2.2, P 7.1.2.3.
E. Leybold's Nachfolger.

Debye-Scherrer Photography



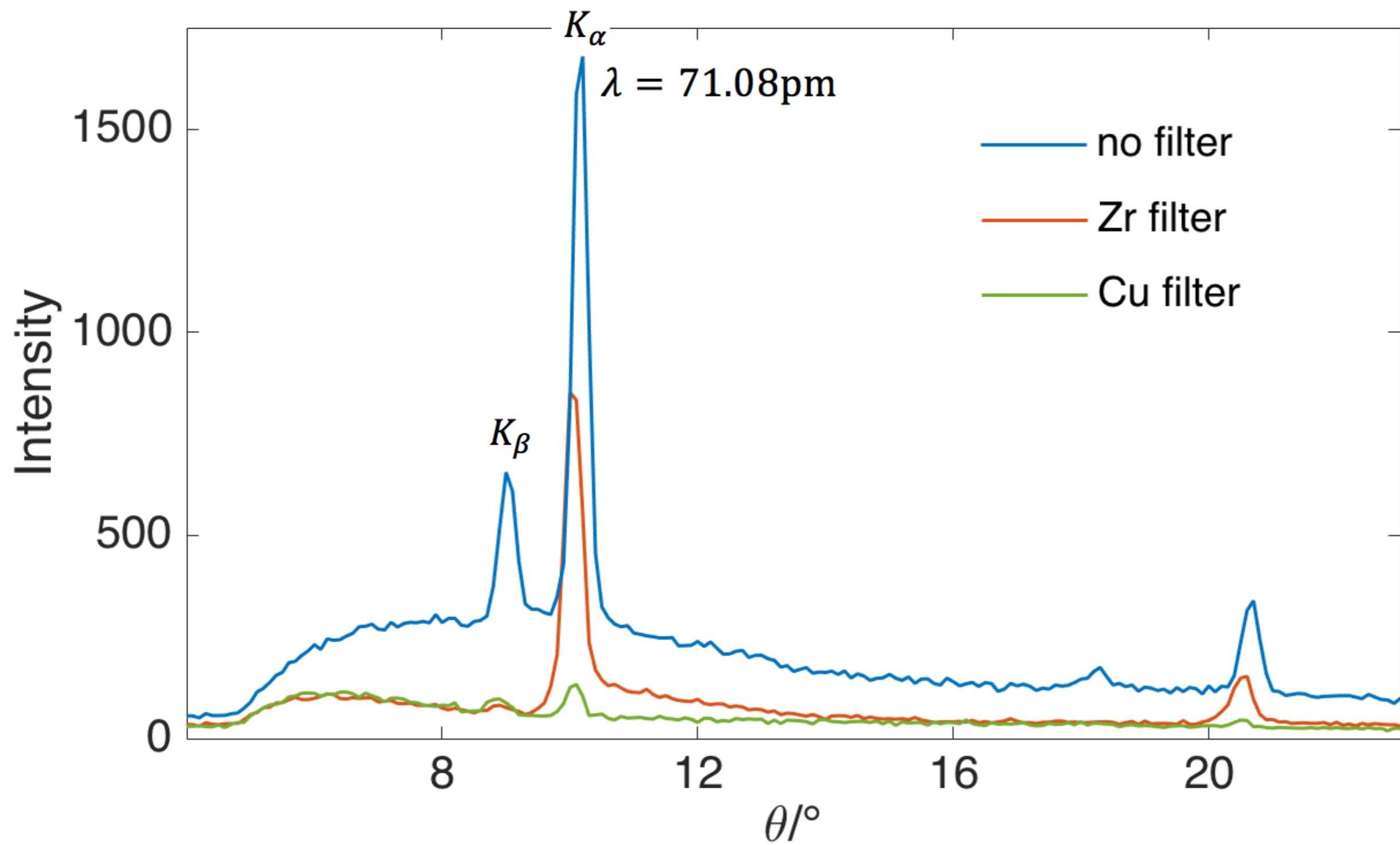
a
X-ray Tube

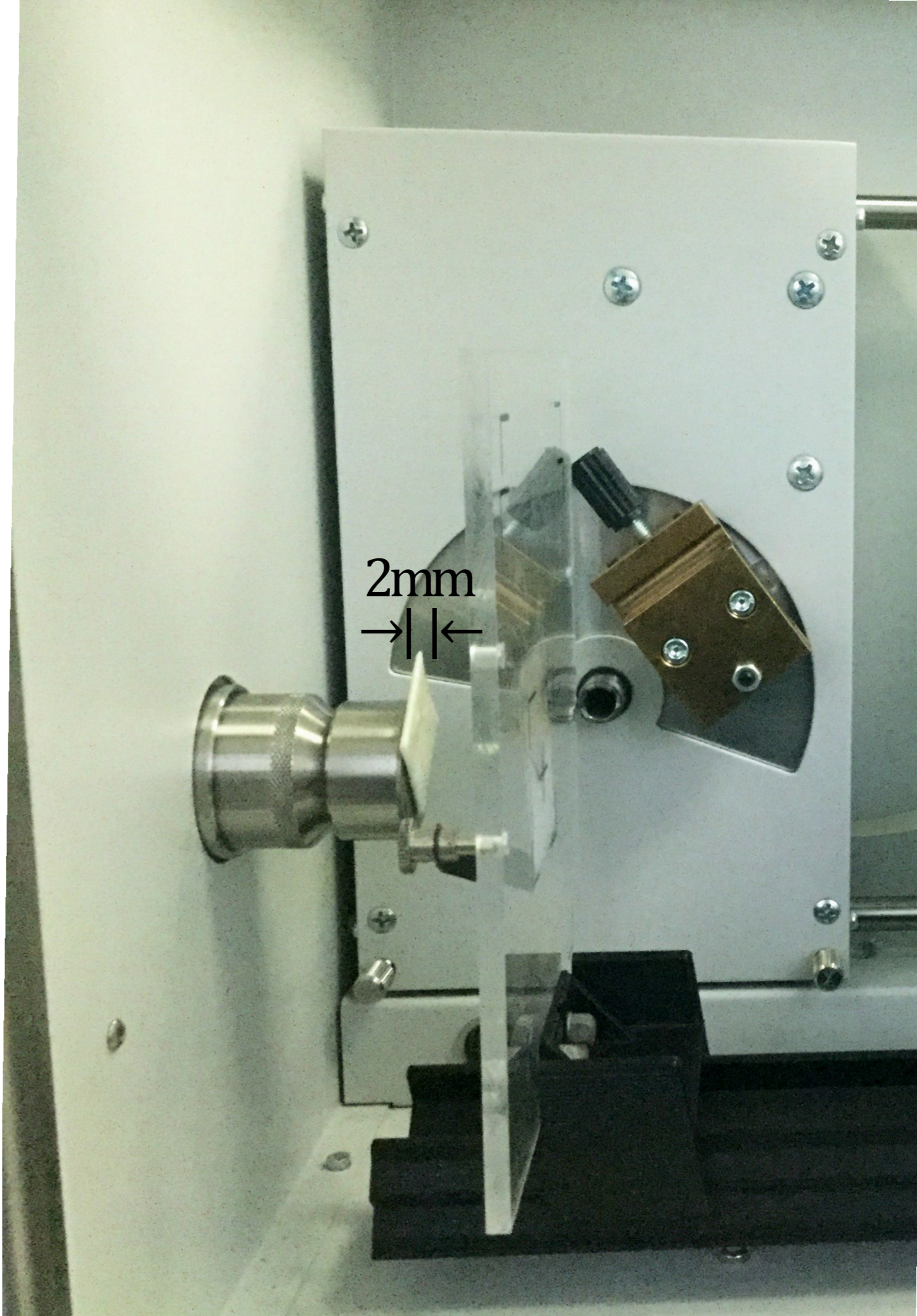
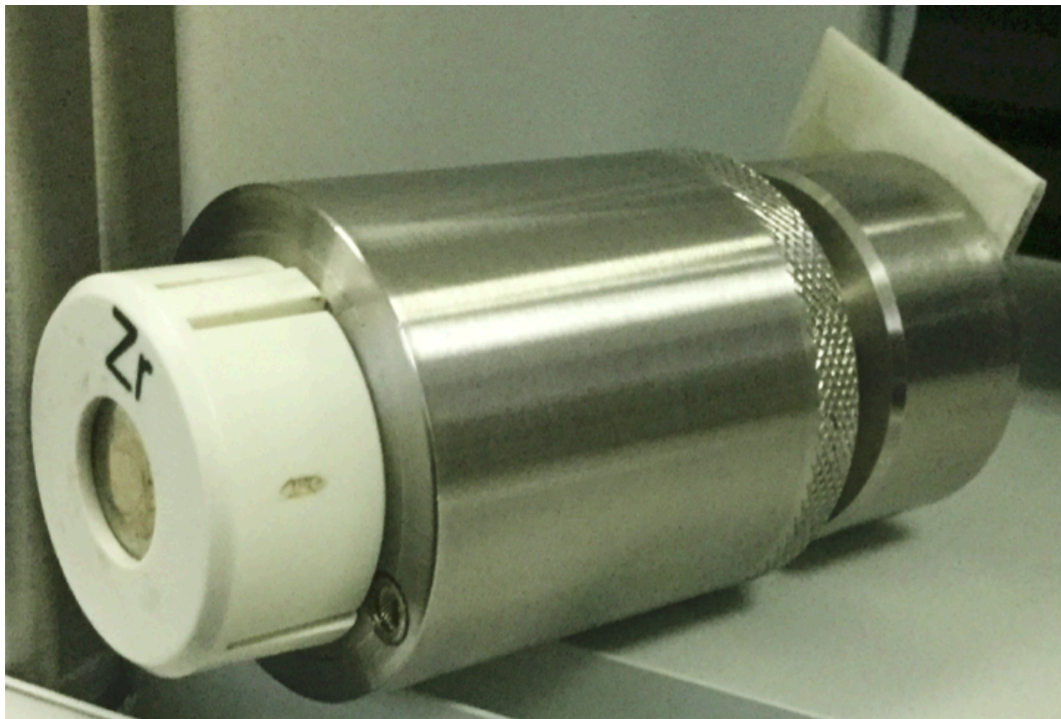
b
Zr Filter

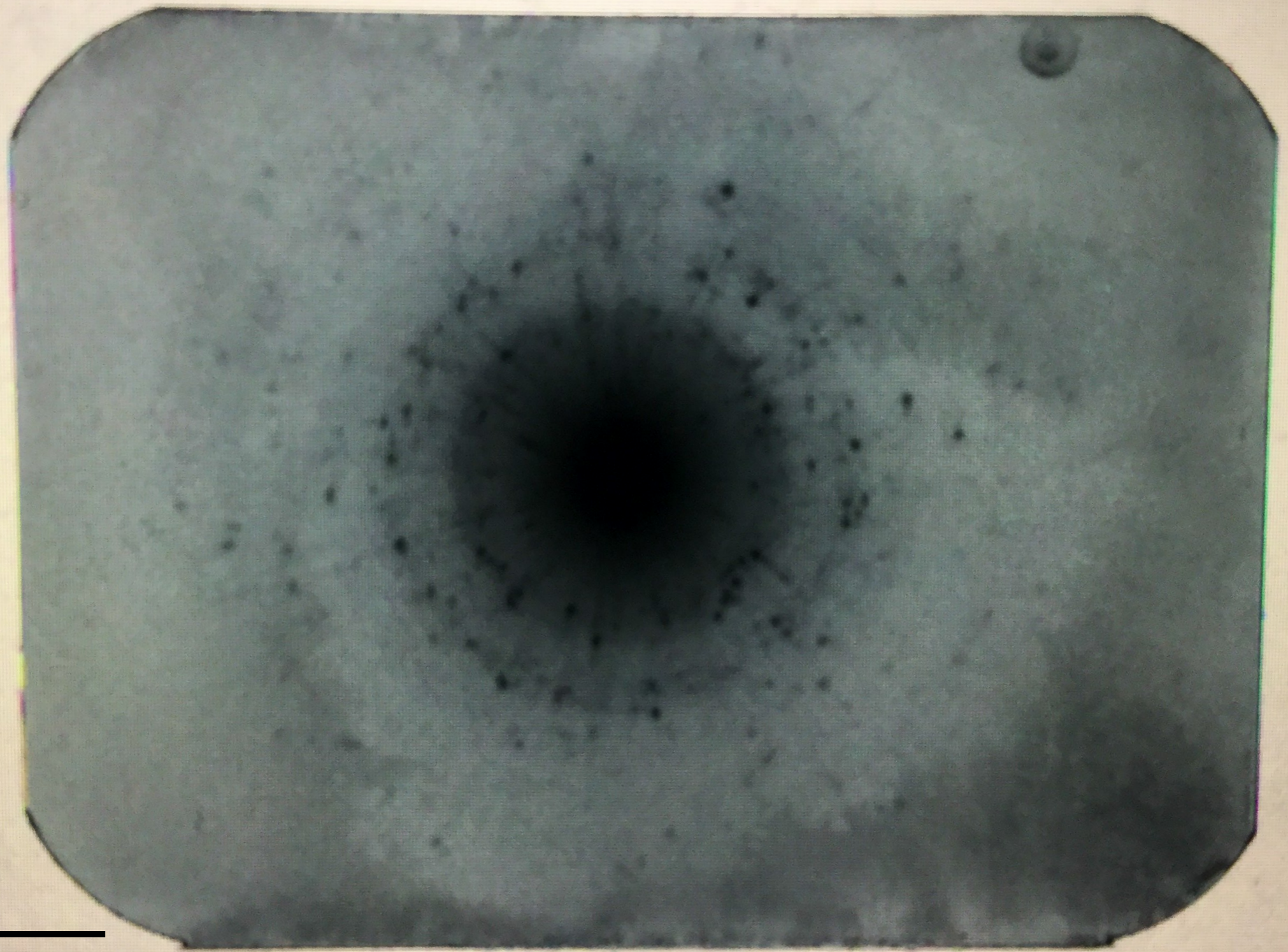
c
Collimator

d
Powder

e
Film

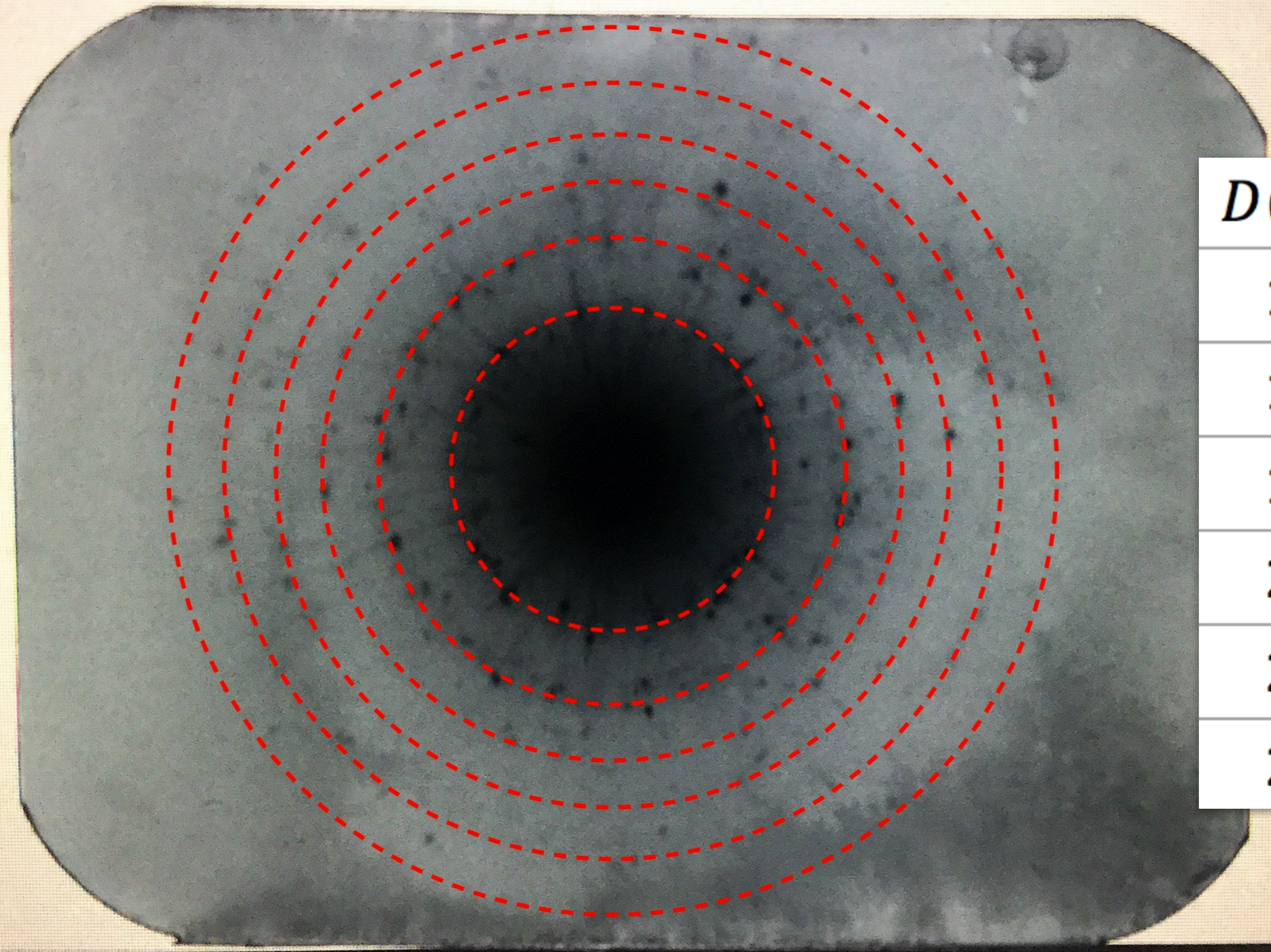




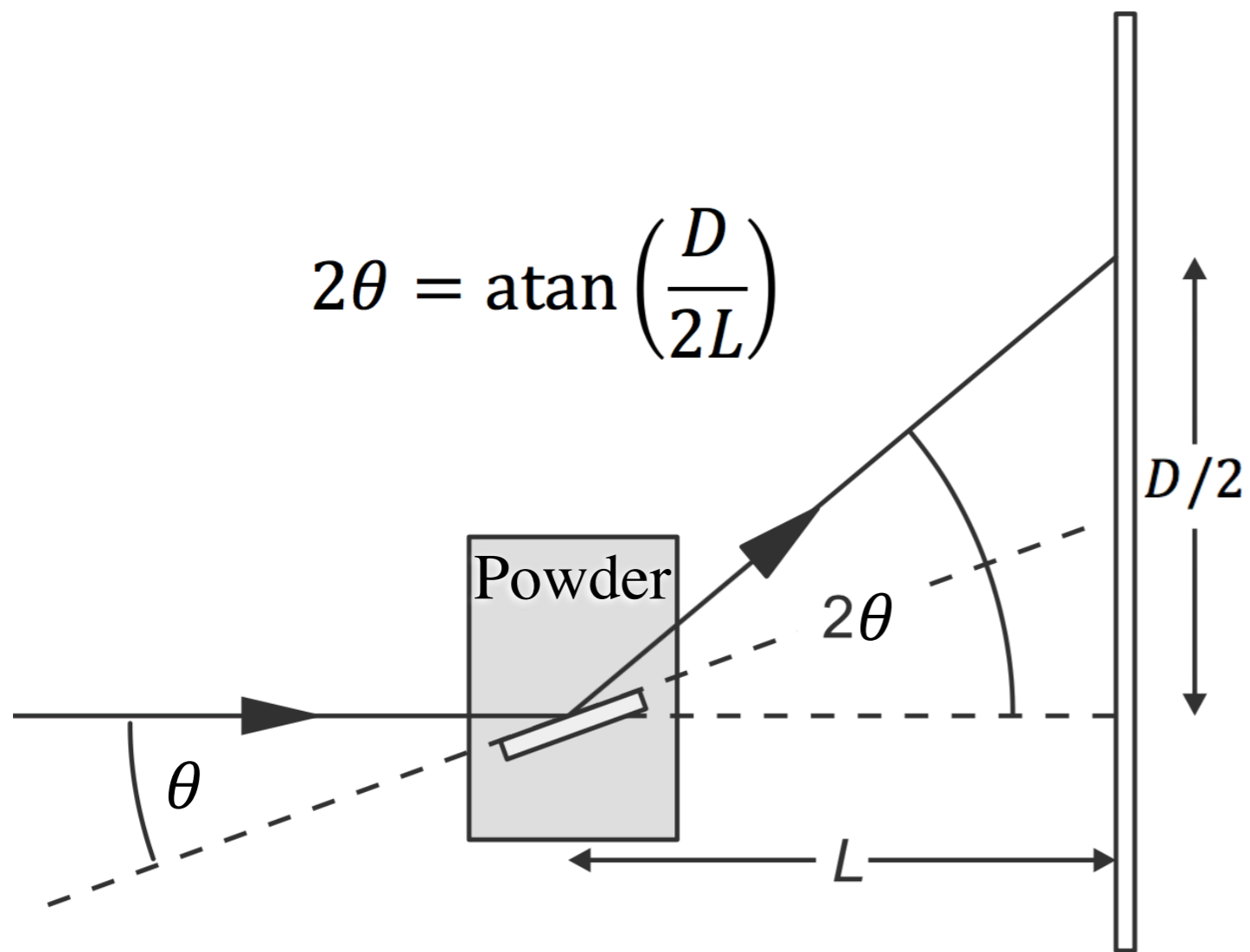


1cm

$L = 20\text{mm}$ *Time = 2h*



$D(\text{mm})$
1.06
1.56
1.94
2.30
2.62
2.96



$$d = \frac{2\pi}{|\mathbf{g}|} = \frac{a_0}{\sqrt{Z}}$$

$$Z = h^2 + k^2 + l^2$$

$$d = \frac{n\lambda}{2 \sin \theta}$$

$$\left(\frac{d_1}{d}\right)^2 = \frac{Z}{Z_1}$$

$$d = \frac{\lambda}{2 \sin\left(\frac{1}{2} \arctan \frac{D}{2L}\right)}$$

$$\left(\frac{d_1}{d}\right)^2 = \frac{Z}{Z_1}$$

D (mm)	d (pm)	$(d_1/d)^2$	Z/Z_1
1.06	275.2	1	1
1.56	192.2	2.1	2
1.94	158.7	3.0	3
2.30	137.8	4.0	4
2.62	125.0	4.9	5
2.96	113.5	5.9	6

$\{hkl\}$	Z
111	3
200	4
220	8
311	11
222	12
400	16
331	19
420	20
422	24
333	27
511	27
440	32
600	32

$$S = \begin{cases} 4(f_{Na} + f_{Cl}) & hkl \text{ all even} \\ 4(f_{Na} - f_{Cl}) & hkl \text{ all odd} \\ 0 & hkl \text{ mixed} \end{cases}$$

$$Z_1 = 4$$

$D(\text{mm})$	$d(\text{pm})$	Z/Z_1
1.06	275.2	1
1.56	192.2	2
1.94	158.7	3
2.30	137.8	4
2.62	125.0	5
2.96	113.5	6

{hkl}	Z
111	3
200	4
220	8
311	11
222	12
400	16
331	19
420	20
422	24
333	27
511	27
440	32
600	32

$$S = \begin{cases} 4(f_{Na} + f_{Cl}) & hkl \text{ all even} \\ 4(f_{Na} - f_{Cl}) & hkl \text{ all odd} \\ 0 & hkl \text{ mixed} \end{cases}$$

$$Z_1 = 4$$

$$a_0 = \sqrt{Z}d$$

D(mm)	d(pm)	Z/Z ₁	a ₀
1.06	275.2	1	550.4
1.56	192.2	2	543.6
1.94	158.7	3	549.8
2.30	137.8	4	551.2
2.62	125.0	5	559.0
2.96	113.5	6	556.0

$$d = \frac{\lambda}{2 \sin\left(\frac{1}{2} \arctan \frac{D}{2L}\right)}$$

$$a_0 = \mathbf{551.7 \text{ pm}}$$

$$a_{NaCl} = 564.02 \text{ pm}$$

